

# *Cross section ratios as a precision tool for $t\bar{t}\gamma$*

*Malgorzata Worek*



# Plan

- ⌘ Motivation for  $t\bar{t}\gamma$
- ⌘ Status of theoretical predictions for  $t\bar{t}\gamma$
- ⌘ NWA vs. off-shell effects  $\rightarrow t\bar{t} \& t\bar{t}j$
- ⌘ Results for  $t\bar{t}\gamma$  in di-lepton channel
- ⌘ Predictions for  $t\bar{t}\gamma/t\bar{t}$
- ⌘ Summary & Outlook

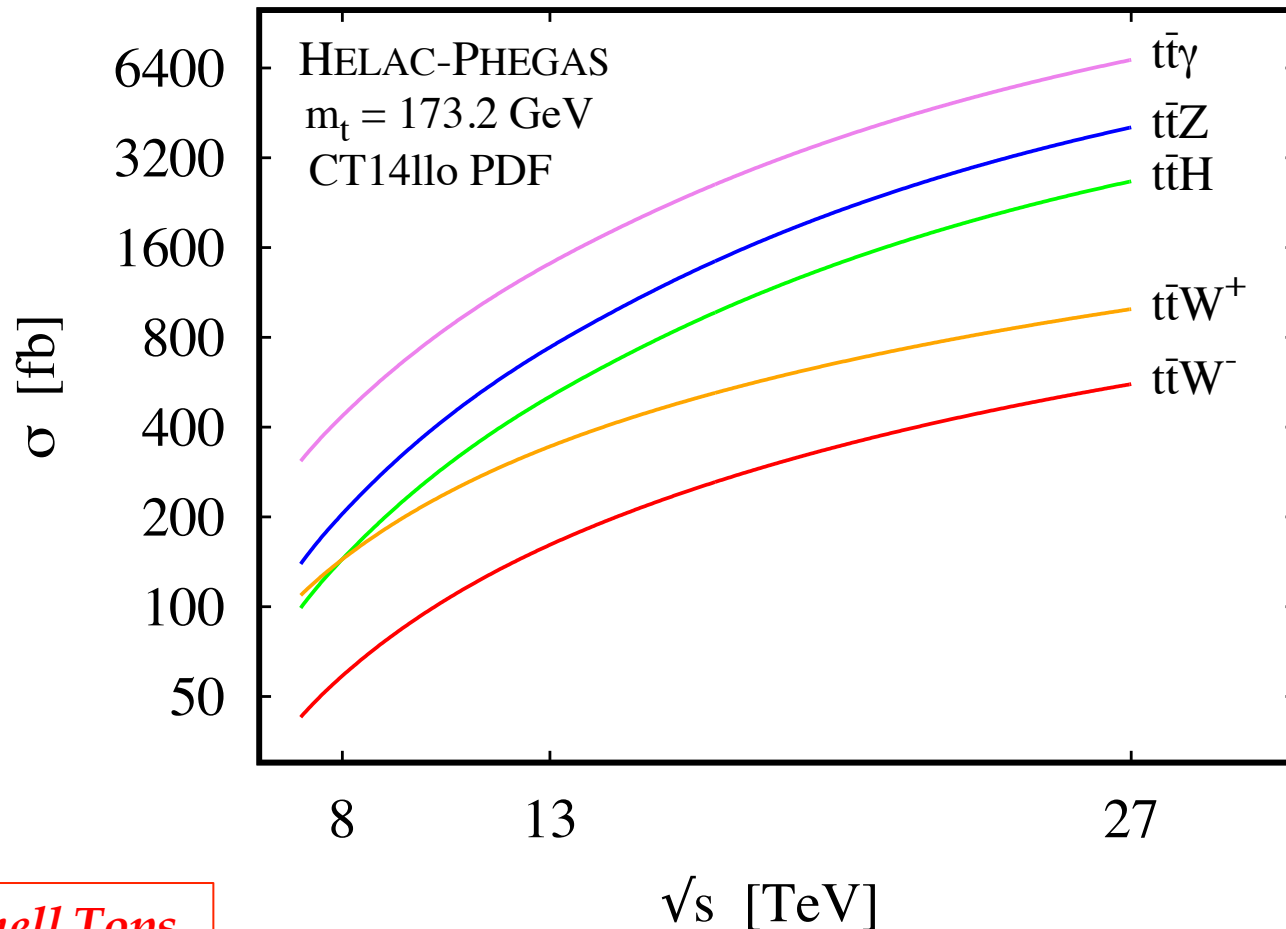
## *Collaborators:*

- *G. Bevilacqua (University of Debrecen, Hungary)*
- *H. B. Hartanto (University of Durham, UK)*
- *M. Kraus (Florida State University, USA)*
- *T. Weber (RWTH Aachen University, Germany)*

# Motivations For $t\bar{t}\gamma$

⌘ Besides  $t\bar{t}$  &  $t\bar{t}j$  more exclusive final states can be accessed @ LHC

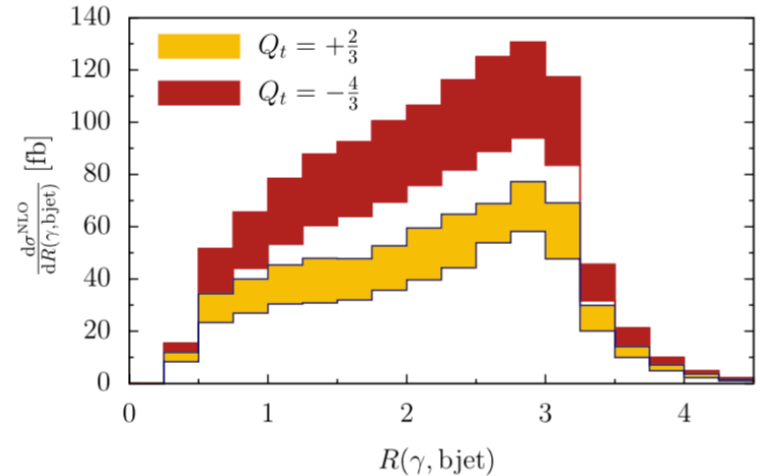
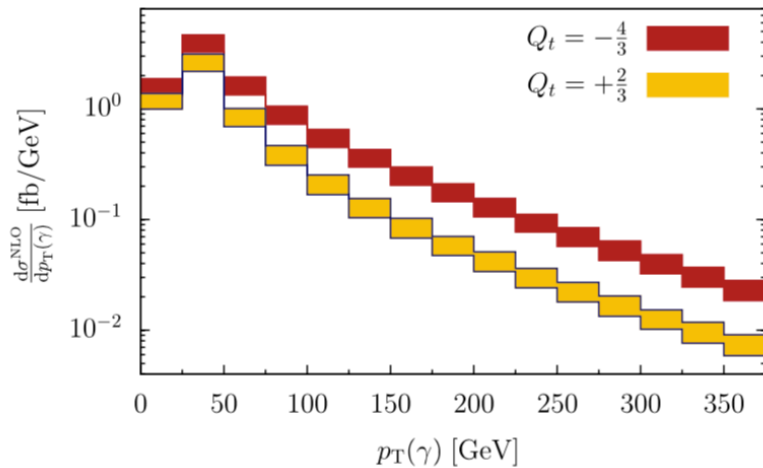
$t\bar{t}\gamma, t\bar{t}Z, t\bar{t}H, t\bar{t}W^\pm$  @ LHC



*On-shell Tops*

# Motivations For $t\bar{t}\gamma$

- ⌘  $t\bar{t}V$  cross sections much smaller than  $t\bar{t}(j)$
- ⌘ *Information on couplings*  $\rightarrow \gamma, Z, H, W^\pm$
- ⌘  $\sigma_{t\bar{t}\gamma}$  direct way to measure *top quark charge @ LHC*  $\rightarrow \sigma_{t\bar{t}\gamma} \sim Q_t^2 @ LHC$
- ⌘  $Q_t = +\frac{2}{3}$  with  $CL \geq 5\sigma @ LHC$   $\rightarrow$  Indirectly from  $Q_t = Q_W - Q_{b\text{-jet}}$  in  $t\bar{t}$
- ⌘ *Exotic physics scenarios*  $\rightarrow$  top-like quarks with  $Q_t \neq +\frac{2}{3}$



$$pp \rightarrow t\bar{t}\gamma \rightarrow \ell^+ \nu_e b\bar{b} j j \gamma @ 14 \text{ TeV LHC}$$

*Melnikov, Schulze, Scharf '11*

# Motivations For $t\bar{t}\gamma$

- ⌘ *Probe the strength and the structure of  $t\bar{t}\gamma$  vertex*  $\rightarrow$  SM + contributions from dimension-six effective operators  $\rightarrow$  Constrains on anomalous couplings

$$\mathcal{L}_{t\bar{t}\gamma} = -eQ_t\bar{t}\gamma^\mu t A_\mu - e\bar{t}\frac{i\sigma^{\mu\nu}(p_t - p_{\bar{t}})_\nu}{m_t}(d_V^\gamma + id_A^\gamma\gamma_5)t A_\mu$$

- ⌘ Measure *cross section ratio* (also differential ratios)

*Aguilar-Saavedra '09  
Schulze, Soreq '16*

$$\mathcal{R} = \frac{\sigma_{pp \rightarrow t\bar{t}\gamma}}{\sigma_{pp \rightarrow t\bar{t}}}$$

*Bevilacqua, Hartanto, Kraus, Weber, Worek '18*

- ★ More stable against radiative corrections
  - ★ Reduced scale dependence  $\rightarrow$  Various uncertainties cancel in ratio
  - ★ Enhanced predictive power  $\rightarrow$  Interesting to probe new physics @ LHC
- ⌘ Top quark charge *asymmetry, differential top quark charge asymmetries, ...*

*Aguilar-Saavedra, Alvarez, Juste, Rubbo '14*

# Theoretical Predictions For $t\bar{t}$

⌘ NLO corrections for on-shell top quarks → General idea about size of NLO corrections. Can not provide reliable description of top quark decay products and radiation pattern

★ *NLO QCD*

*Duan, Ma, Zhang, Han, Guo, Wang '09 '11*

*Maltoni, Pagani, Tsinikos '15*

★ *NLO electroweak*

*Duan, Zhang, Wang, Song, Li '16*

⌘ For more realistic studies decays are needed

★ *NLO QCD for on-shell top quarks + PS* → Top decays in parton shower approximation, omitting photon emission in PS evolution & omitting  $t\bar{t}$  spin correlations

*Kardos, Trocsanyi '14*

★ *NLO QCD in NWA* → NLO QCD corrections to top production & decays, photon emission of top quark and of top quark decay product &  $t\bar{t}$  spin correlations included

*Melnikov, Schulze, Scharf '11*

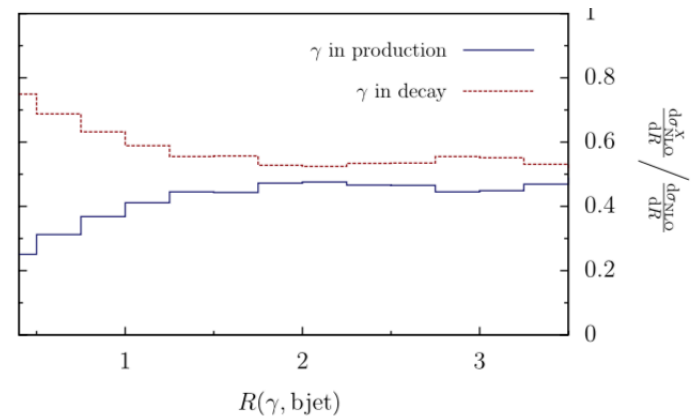
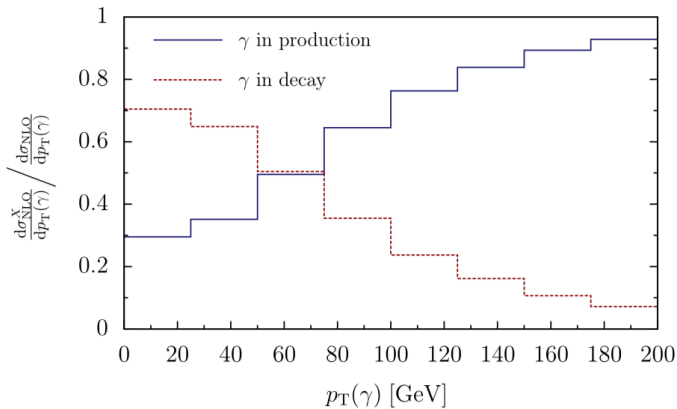
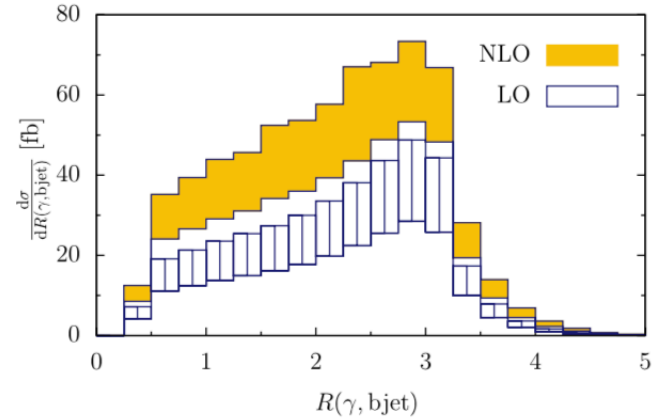
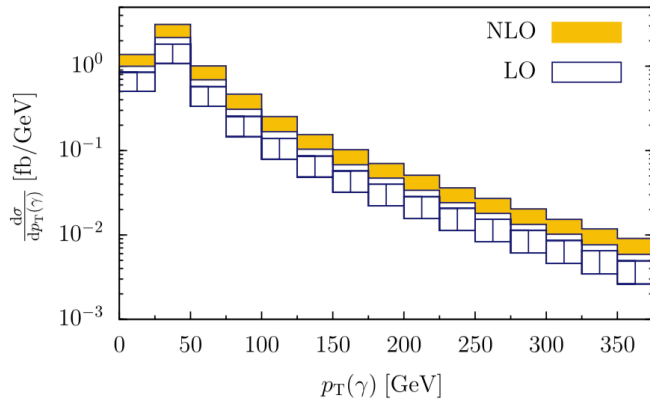
★ *NLO QCD complete off-shell effects of top quarks* → resonant & non-resonant diagrams, interferences and off-shell effects of the top quarks

*Bevilacqua, Hartanto, Kraus, Weber, Worek '18*

# $t\bar{t}\gamma$ in NWA @ LHC

*Melnikov, Schulze, Scharf '11*

$pp \rightarrow t\bar{t}\gamma \rightarrow \ell^+ \nu_\ell b\bar{b}j\gamma$  @ 14 TeV LHC



⌘ Large fraction of isolated photons comes from radiative decay of tops

$$\sigma^{\text{NLO}} = 138 \text{ fb}$$

$$\sigma_{\gamma\text{-Prod.}}^{\text{NLO}} = 60.9 \text{ fb}$$

$$\sigma_{\gamma\text{-Dec.}}^{\text{NLO}} = 77.2 \text{ fb}$$

# How Good Is NWA ?

- ❖ In NWA tops are restricted to on-shell states
- ❖ Approximation is controlled by the ratio  $\Gamma_t/m_t \approx 0.8\%$
- ❖ Should be accurate for sufficiently inclusive observables
- ❖ *Off-shell effects for integrated  $\sigma_{tt}$  @ few % level @ NLO in QCD*

*Off-shell Tops*

|                           |   |
|---------------------------|---|
| <i>tt (di-lepton)</i>     | <i>Denner, Dittmaier, Kallweit, Pozzorini '11 '12<br/>Bevilacqua, Czakon, van Hameren, Papadopoulos, Worek '11<br/>Denner, Pellen '16 (EW)<br/>Jezo, Lindert, Nason, Oleari, Pozzorini '16 (PS)</i> |
| <i>tt (semi-leptonic)</i> | <i>Denner, Pellen '18</i>   |
| <i>ttH (di-lepton)</i>    | <i>Denner, Feger '15<br/>Denner, Lang, Pellen, Uccirati '17 (EW+QCD)</i>  |
| <i>ttj (di-lepton)</i>    | <i>Bevilacqua, Hartanto, Kraus, Worek '16 '18</i>   |
| <i>tty (di-lepton)</i>    | <i>Bevilacqua, Hartanto, Kraus, Weber, Worek '18 '19</i>  |



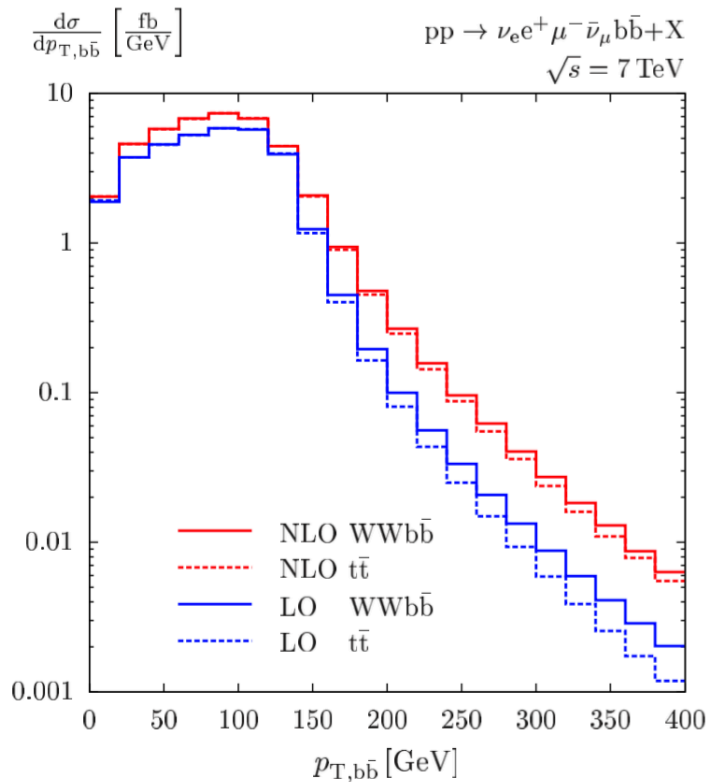
# NWA & Off-Shell Effects

❖ Off-shell results vs. results with (spin-correlated) NWA

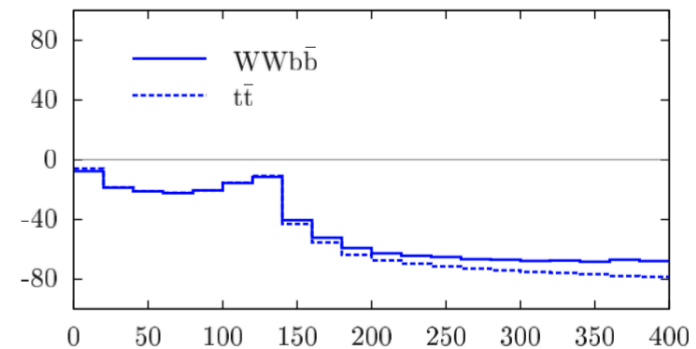
*Off-shell Tops*

❖ *Tens of per cent* in phase-space regions where  $t\bar{t}$  suppressed as signal

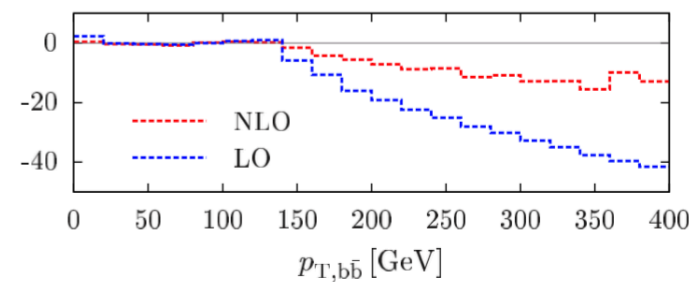
❖ Important as background to *Higgs & BSM searches*



LO/NLO - 1 [%]



$t\bar{t}/WWb\bar{b} - 1$  [%]



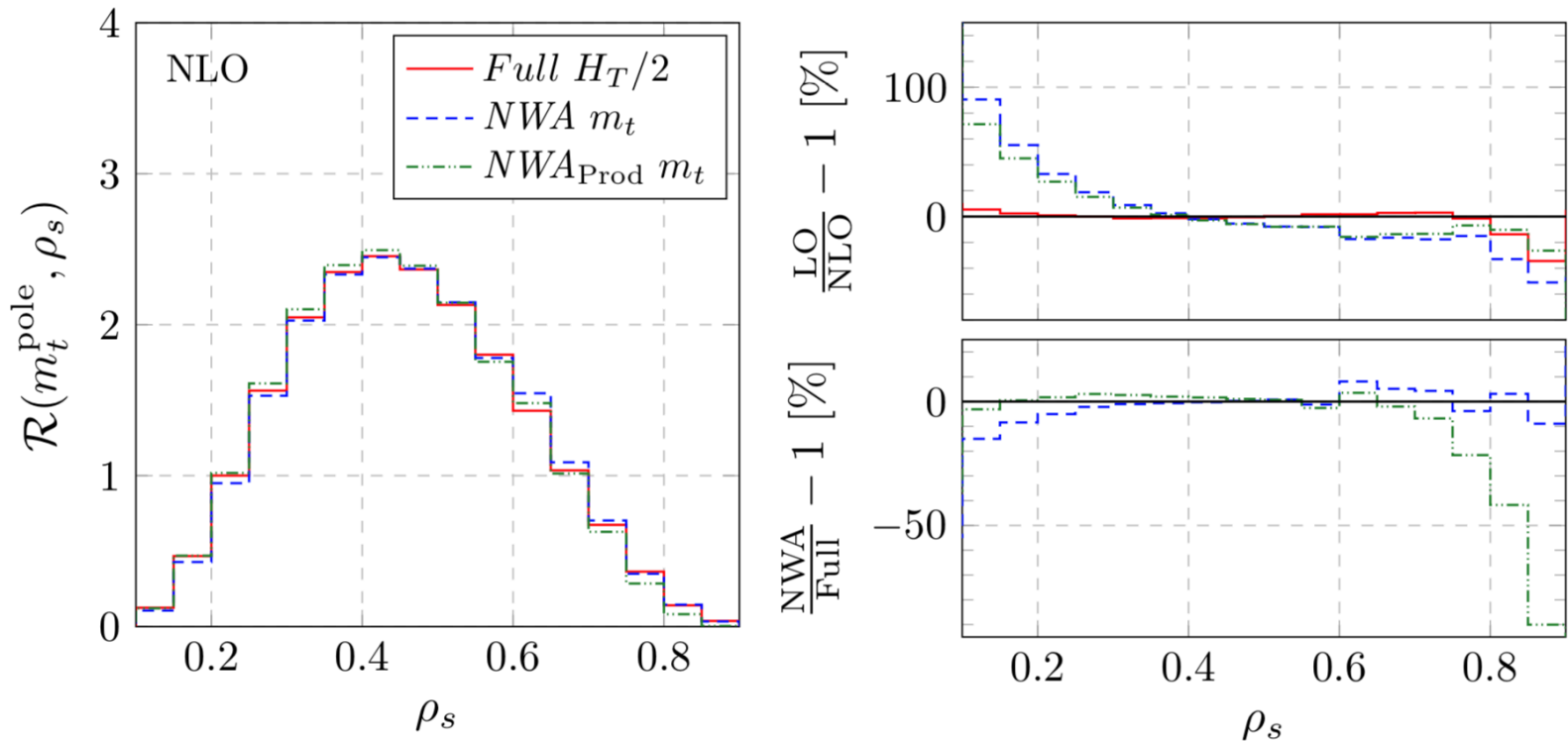
# NWA & Off-Shell Effects

❖ Observable used for a recent *top quark mass determination*

**Off-shell, NWA**

$pp \rightarrow t\bar{t}j \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}j$  @ LHC<sub>13TeV</sub>

*Bevilacqua, Hartanto, Kraus, Schulze, Worek '18*



$$\mathcal{R}(m_t^{\text{pole}}, \rho_s) = \frac{1}{\sigma_{t\bar{t}j}} \frac{d\sigma_{t\bar{t}j}}{d\rho_s}(m_t^{\text{pole}}, \rho_s)$$

$$\rho_s = \frac{2m_0}{M_{t\bar{t}j}}$$

*Alioli, Fernandez, Fuster, Irlles, Moch, Uwer, Vos '13*

# NWA & Off-Shell Effects

25 fb<sup>-1</sup>

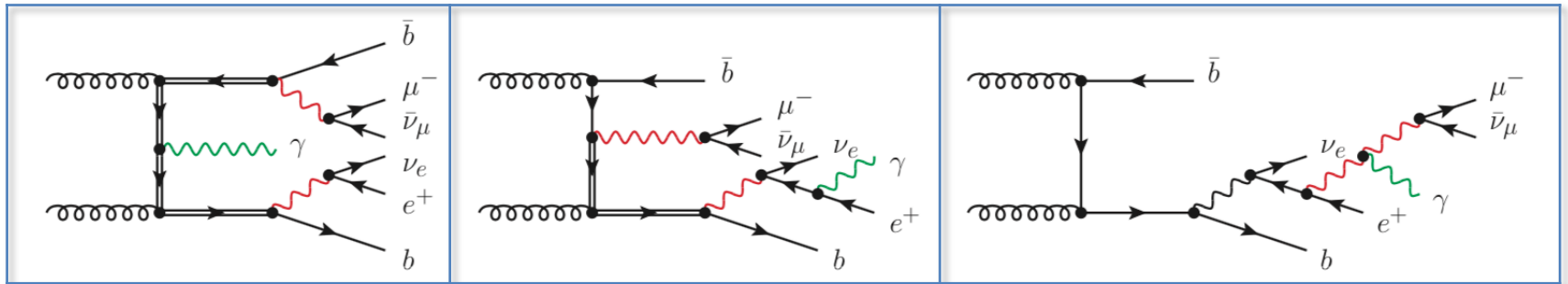
$pp \rightarrow t\bar{t}j \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}j$  @ LHC<sub>13TeV</sub>

| Theory, NLO QCD<br>CT14 PDF                          | $m_t^{\text{out}} \pm \delta m_t^{\text{out}}$<br>[GeV] | Averaged<br>$\chi^2/\text{d.o.f.}$ | Probability<br>$p\text{-value}$   | $m_t^{\text{in}} - m_t^{\text{out}}$<br>[GeV] |
|--|---|------------------------------------|-----------------------------------|---|
| <i>31 bins</i>                                       |   |                                    |                                   |   |
| <i>Full, <math>\mu_0 = H_T/2</math></i>              | $173.09 \pm 0.42$                                       | 1.04                               | 0.41 (0.8 $\sigma$ )              | +0.11   |
| <i>Full, <math>\mu_0 = E_T/2</math></i>              | $172.45 \pm 0.39$                                       | 1.12                               | 0.30 (1.0 $\sigma$ )              | +0.75   |
| <i>Full, <math>\mu_0 = m_t</math></i>                | $173.76 \pm 0.40$                                       | 1.87                               | 0.003 (3.0 $\sigma$ )             | -0.56   |
| <i>NWA, <math>\mu_0 = m_t</math></i>                 | $175.65 \pm 0.31$                                       | 2.99                               | $7 \cdot 10^{-8}$ (5.4 $\sigma$ ) | -2.45   |
| <i>NWA<sub>Prod.</sub>, <math>\mu_0 = m_t</math></i> | $169.59 \pm 0.30$                                       | 3.10                               | $2 \cdot 10^{-8}$ (5.6 $\sigma$ ) | +3.61   |
| <i>5 bins</i>  |   |                                    |                                   |   |
| <i>Full, <math>\mu_0 = H_T/2</math></i>              | $173.08 \pm 0.40$                                       | 0.94                               | 0.44 (0.8 $\sigma$ )              | +0.12   |
| <i>Full, <math>\mu_0 = E_T/2</math></i>              | $172.48 \pm 0.38$                                       | 1.58                               | 0.18 (1.3 $\sigma$ )              | +0.72   |
| <i>Full, <math>\mu_0 = m_t</math></i>                | $173.75 \pm 0.40$                                       | 6.76                               | $2 \cdot 10^{-5}$ (4.3 $\sigma$ ) | -0.55   |
| <i>NWA, <math>\mu_0 = m_t</math></i>                 | $175.49 \pm 0.30$                                       | 5.31                               | $2 \cdot 10^{-4}$ (3.7 $\sigma$ ) | -2.29   |
| <i>NWA<sub>Prod.</sub>, <math>\mu_0 = m_t</math></i> | $169.39 \pm 0.47$                                       | 3.42                               | $8 \cdot 10^{-3}$ (2.6 $\sigma$ ) | +3.81   |

# NWA & Off-Shell Effects

❖ Feynman Diagrams → 628 @ LO for gg channel

$$t\bar{t}\gamma + X @ \mathcal{O}(\alpha_s^2\alpha^5)$$

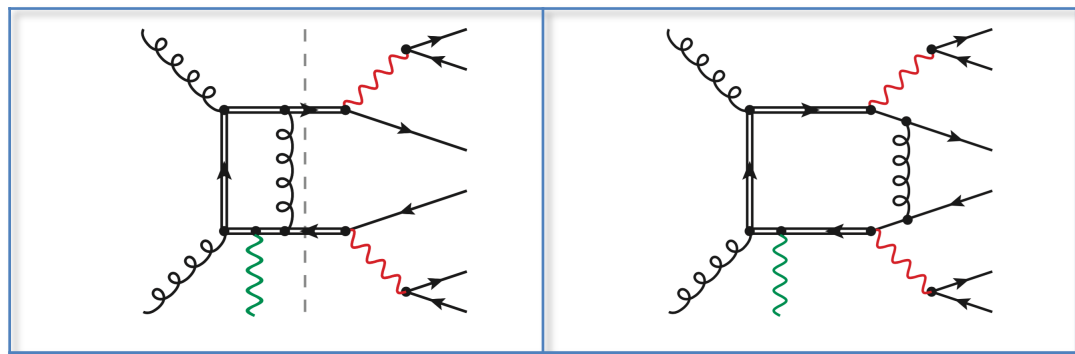


❖ NLO → 4348 real emission & 36032 @ 1-loop for gg channel

❖ Most complicated → 90 heptagons & 958 hexagons

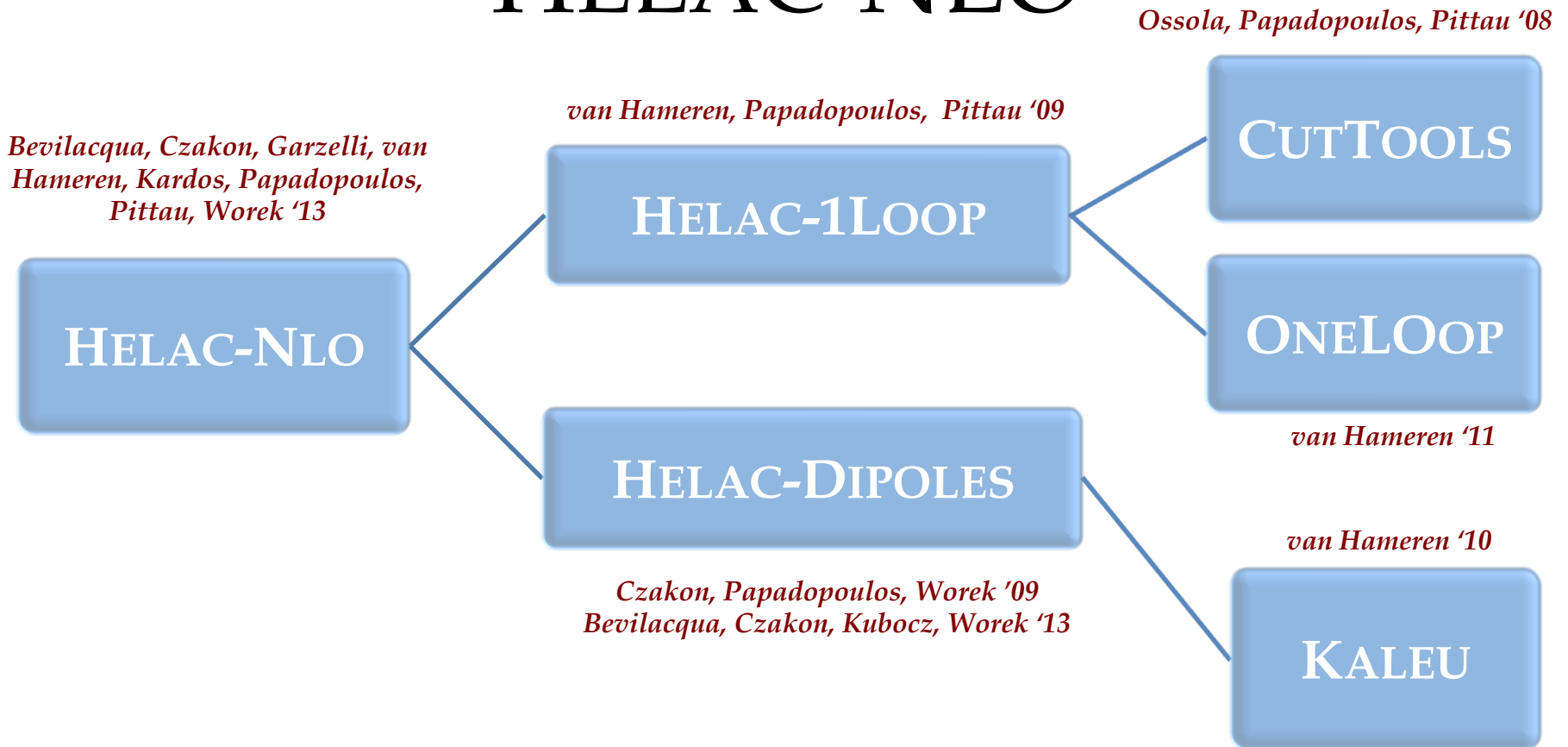
$$t\bar{t}\gamma + X @ \mathcal{O}(\alpha_s^3\alpha^5)$$

*tty in NWA  
up to pentagons*



*tty full  
up to heptagons*

# HELAC-NLO



## ⌘ Output:

- ❖ theoretical predictions are stored in the form of the **Ntuples Event Files**
- ❖ modified **Les Houches & ROOT Event Files**
- ❖ kinematical cuts can be changed
- ❖ new observables can be defined
- ❖ renormalization or factorization scales and PDF sets can be changed

# Setup for $t\bar{t}\gamma$

⌘ Different lepton generations

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma @ \text{LHC}_{13\text{TeV}}$$

⌘ Interference effects neglected  $\rightarrow$  *Per-mille level @ LO*

⌘ Contribution from b quarks in the initial state neglected  $\rightarrow$  *Effect < 0.1% @ LO*

⌘ *2 b-jets, one photon, two charged leptons &  $p_T^{\text{miss}}$*

⌘ Photon:  $p_T(\gamma) > 25 \text{ GeV}, |y_\gamma| < 2.5$

⌘ Isolation condition for photon  $\rightarrow$  Reject event if  $R \leq R_{\gamma j}$  with  $R_{\gamma j} = 0.4$

*Fraxione '98*

$$\sum_i E_{T,i} \Theta(R - R_{\gamma i}) \leq E_{T,\gamma} \left( \frac{1 - \cos(R)}{1 - \cos(R_{\gamma j})} \right)$$

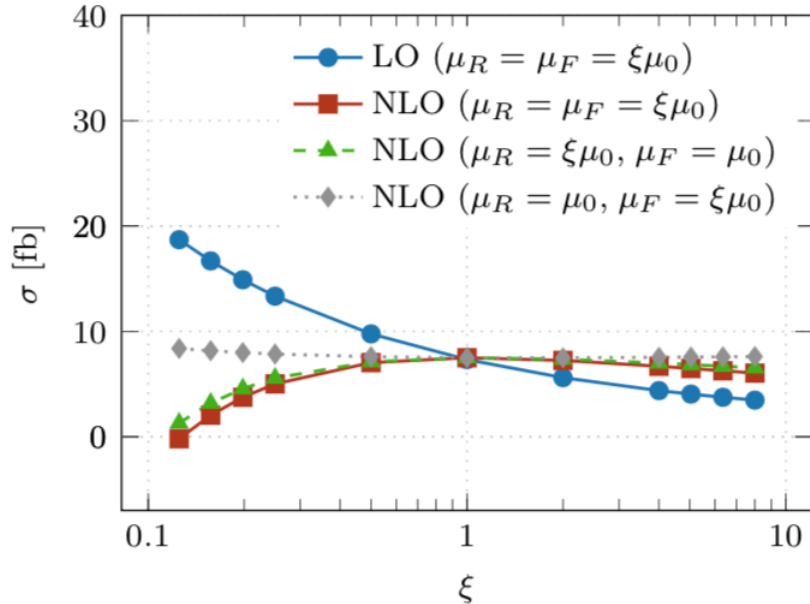
⌘ For hard photon  $\alpha = \alpha(0) = 1/137 \rightarrow$  *Predictions decreased by 3%*

⌘ Electroweak coupling in the  $G_\mu$  scheme  $\rightarrow$  account for some electroweak effects

⌘ Kinematics-independent & kinematic-dependent scale:  $\mu_0 = m_t/2, H_T/4$

# tty with $H_T$

Bevilacqua, Hartanto, Kraus, Weber, Worek '18



$$\mu_R \neq \mu_F, \quad 0.5 < \mu_R/\mu_F < 2$$

$$\mu_0 = H_T/4, \text{ CT14}$$

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma \text{ @ LHC}_{13\text{TeV}}$$

$$\sigma_{pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma}^{\text{LO}}(\text{CT14}, \mu_0 = H_T/4) = 7.32^{+2.44(33\%)}_{-1.71(23\%)} \text{ fb},$$

$$\sigma_{pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma}^{\text{NLO}}(\text{CT14}, \mu_0 = H_T/4) = 7.50^{+0.10(1\%)}_{-0.46(6\%)} \text{ fb}.$$

$$H_T = p_{T, e^+} + p_{T, \mu^-} + p_{T, j_b} + p_{T, j_{\bar{b}}} + p_T^{\text{miss}} + p_{T, \gamma}$$

⌘ Positive & small *NLO corrections of 2.5%*

⌘ Theoretical uncertainties  
 → **33% @ LO & 6% @ NLO**

$$\sigma_{pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma}^{\text{NLO}}(\text{CT14}, \mu_0 = m_t/2) = 7.44^{+0.07(1\%)}_{-1.03(14\%)} [\text{scales}]^{+0.05(1\%)}_{+0.28(4\%)} [\text{PDF}] \text{ fb}.$$

# tty with $H_T$

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$  @ LHC<sub>13TeV</sub>

| PDF   | $p_{T,b}$ | $\sigma^{\text{LO}}$ [fb] | $\delta_{\text{scale}}$    | $\sigma^{\text{NLO}}$ [fb] | $\delta_{\text{scale}}$  | $\delta_{\text{PDF}}$    | $\mathcal{K} = \frac{\text{NLO}}{\text{LO}}$ |
|-------|-----------|---------------------------|----------------------------|----------------------------|--------------------------|--------------------------|--|
| CT    | 25        | 10.68                     | +3.54 (33%)<br>-2.49 (23%) | 11.19                      | +0.16 (1%)<br>-0.54 (5%) | +0.32 (3%)<br>-0.35 (3%) | 1.05   |
|       | 30        | 9.58                      | +3.18 (33%)<br>-2.24 (23%) | 9.93                       | +0.14 (1%)<br>-0.54 (5%) | +0.28 (3%)<br>-0.31 (3%) | 1.04   |
|       | 35        | 8.44                      | +2.80 (33%)<br>-1.97 (23%) | 8.69                       | +0.12 (1%)<br>-0.50 (6%) | +0.25 (3%)<br>-0.27 (3%) | 1.03   |
|       | 40        | 7.32                      | +2.45 (33%)<br>-1.71 (23%) | 7.50                       | +0.11 (1%)<br>-0.45 (6%) | +0.22 (3%)<br>-0.23 (3%) | 1.02   |
| MMHT  | 25        | 11.59                     | +4.22 (36%)<br>-2.88 (25%) | 11.29                      | +0.16 (1%)<br>-0.57 (5%) | +0.24 (2%)<br>-0.22 (2%) | 0.97   |
|       | 30        | 10.38                     | +3.78 (36%)<br>-2.58 (25%) | 10.02                      | +0.13 (1%)<br>-0.58 (6%) | +0.22 (2%)<br>-0.19 (2%) | 0.97   |
|       | 35        | 9.12                      | +3.33 (36%)<br>-2.26 (25%) | 8.77                       | +0.11 (1%)<br>-0.54 (6%) | +0.19 (2%)<br>-0.17 (2%) | 0.96   |
|       | 40        | 7.90                      | +2.89 (37%)<br>-1.96 (25%) | 7.57                       | +0.09 (1%)<br>-0.48 (6%) | +0.16 (2%)<br>-0.15 (2%) | 0.96   |
| NNPDF | 25        | 10.78                     | +3.82 (35%)<br>-2.62 (24%) | 11.62                      | +0.17 (1%)<br>-0.58 (5%) | +0.16 (1%)<br>-0.16 (1%) | 1.08   |
|       | 30        | 9.65                      | +3.42 (35%)<br>-2.34 (24%) | 10.31                      | +0.14 (1%)<br>-0.58 (6%) | +0.14 (1%)<br>-0.14 (1%) | 1.07   |
|       | 35        | 8.48                      | +3.01 (35%)<br>-2.05 (24%) | 9.02                       | +0.12 (1%)<br>-0.53 (6%) | +0.12 (1%)<br>-0.12 (1%) | 1.06   |
|       | 40        | 7.34                      | +2.61 (36%)<br>-1.78 (24%) | 7.79                       | +0.10 (1%)<br>-0.48 (6%) | +0.11 (1%)<br>-0.11 (1%) | 1.06   |

*Stability w.r.t.  $p_{T,b}$  cut*

⌘ NLO QCD corrections  
stable against  $p_{T,b}$  cut

⌘ CT14 PDF uncertainties  
similar/smaller than  
difference between  
various PDF sets

⌘ Similar results for  $p_{T,\gamma}$  cut



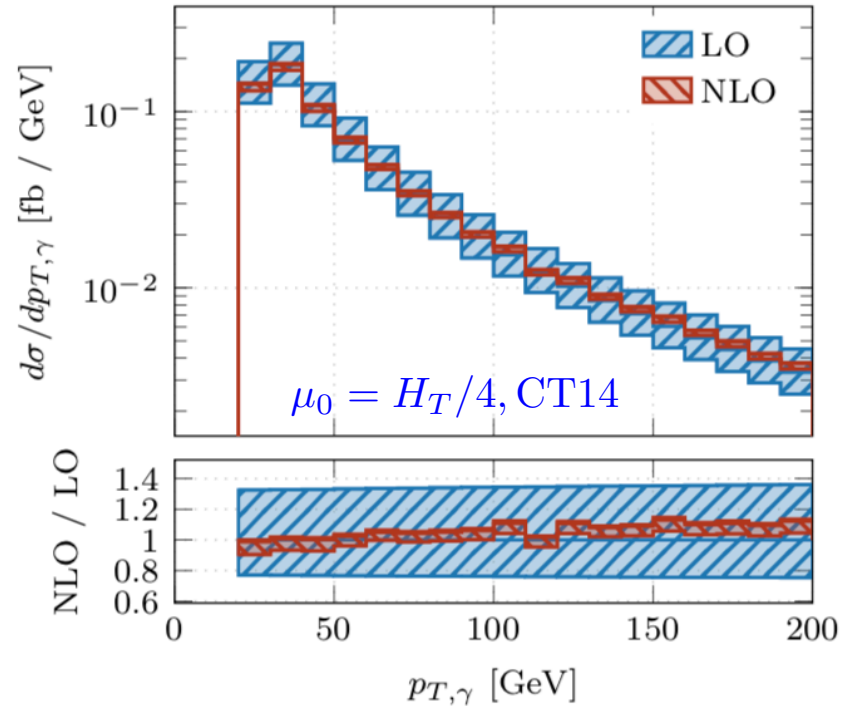
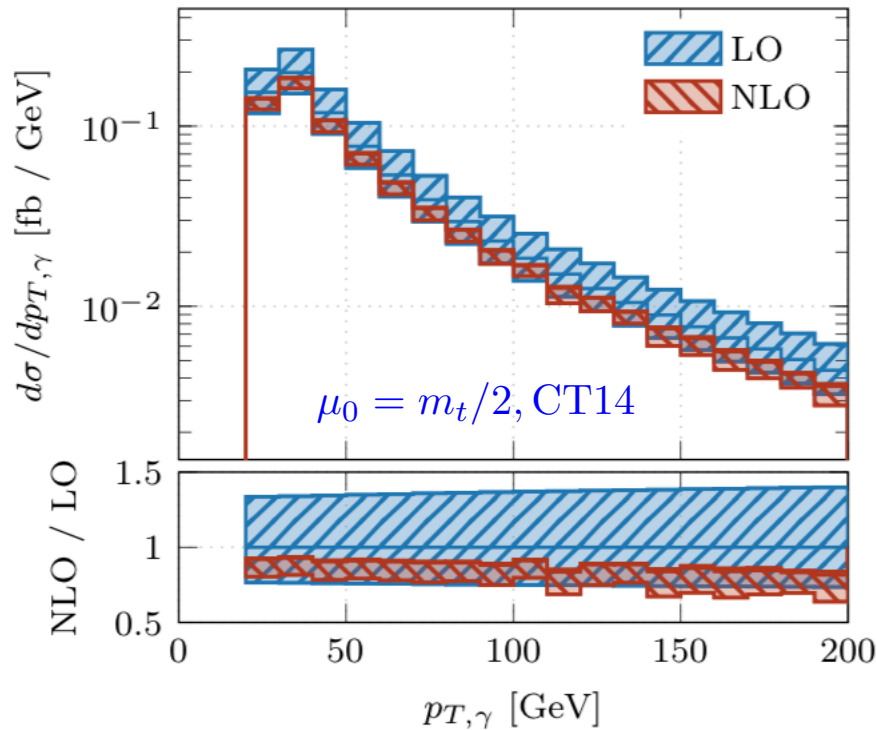
# $t\bar{t}\gamma$ with $m_t$ & $H_T$

LHC<sub>13 TeV</sub>

$p_T(\gamma)$

Bevilacqua, Hartanto, Kraus, Weber, Worek '18

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}\gamma$  @ LHC<sub>13 TeV</sub>



- ⌘ Negative NLO corrections up to 18%
- ⌘ Theoretical error up to  $\pm 22\%$

- ⌘ Positive NLO corrections up to 13%
- ⌘ NLO error bands within LO
- ⌘ Theoretical error up to  $\pm 8\%$

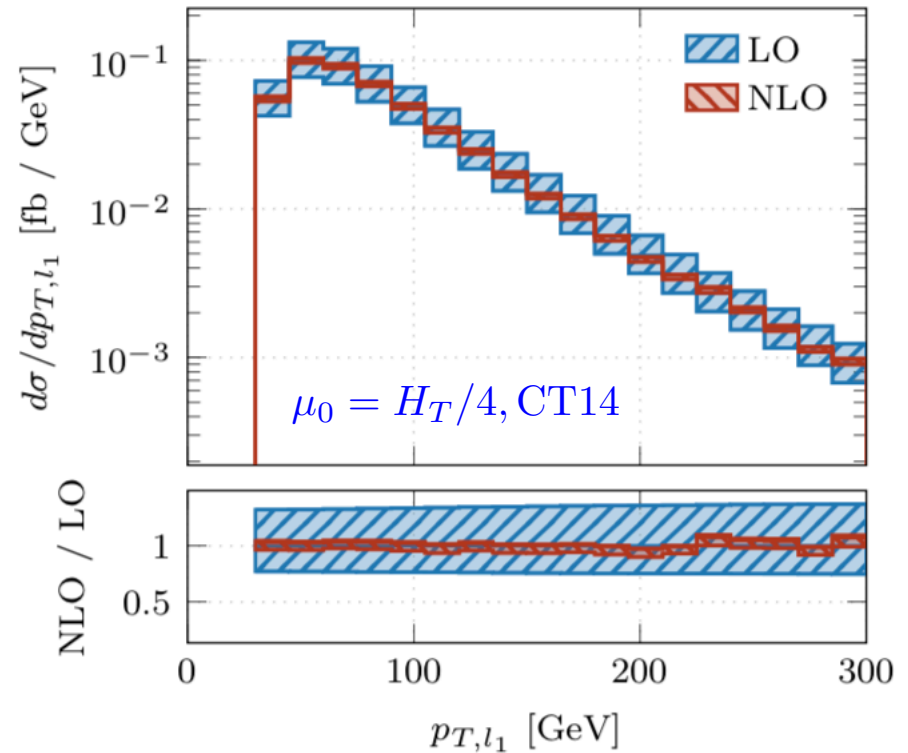
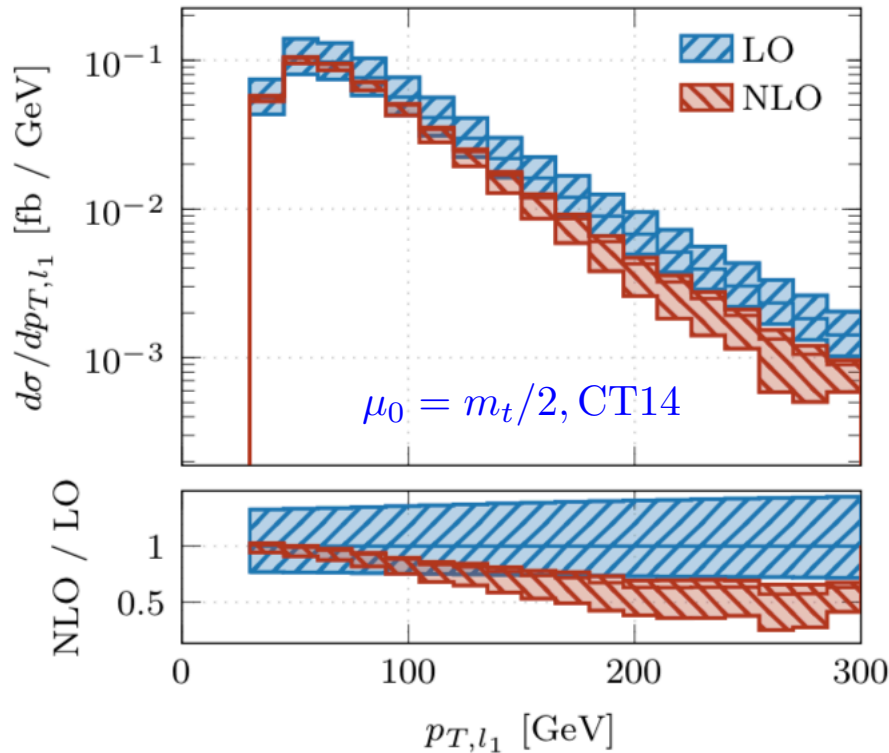
# tty with $m_t$ & $H_T$

$p_T(l_1)$

LHC<sub>13 TeV</sub>

Bevilacqua, Hartanto, Kraus, Weber, Worek '18

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$  @ LHC<sub>13 TeV</sub>



- ⌘ NLO Corrections up to **-43%**
- ⌘ Theoretical uncertainties up to  **$\pm 56\%$**

- ⌘ NLO Corrections up to **+8%**
- ⌘ Error reduced down to  **$\pm 7\%$**

*Dynamical scale very effective in stabilizing perturbative convergence !  
Provides smaller theoretical error !*

# tt̄γ / tt̄

⌘ For fiducial cross section with dynamical scale we have  $\pm 6\%$

⌘ For *differential distributions* we have  $\pm (10\% - 30\%)$

⌘ Can we decrease theoretical error even further for tt̄γ ?

$$\mathcal{R} = \frac{\sigma_{tt\bar{\gamma}}^{\text{NLO}}(\mu_1)}{\sigma_{t\bar{t}}^{\text{NLO}}(\mu_2)}$$

⌘ *Answer is yes!* → with tt̄γ/tt̄ we have  $\pm (1\% - 3\%)$   
for integrated cross section ratio

⌘ *Differential cross section ratios*  $\pm (1\% - 6\%)$

$$\mathcal{R}_X = \left( \frac{d\sigma_{tt\bar{\gamma}}^{\text{NLO}}(\mu_1)}{dX} \right) \left( \frac{d\sigma_{t\bar{t}}^{\text{NLO}}(\mu_2)}{dX} \right)^{-1}$$

⌘ High precision comparable to NNLO QCD results for top quark physics !

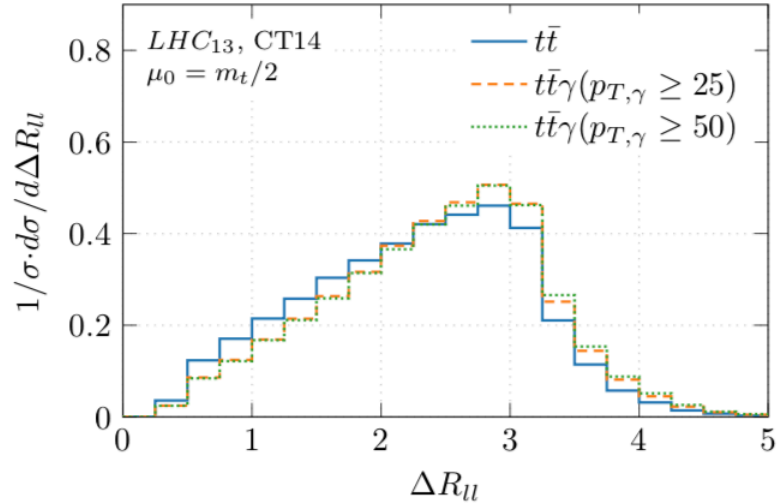
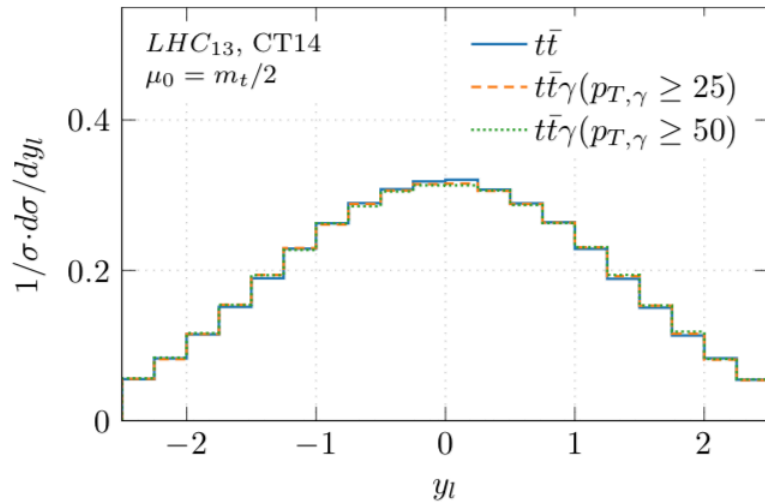
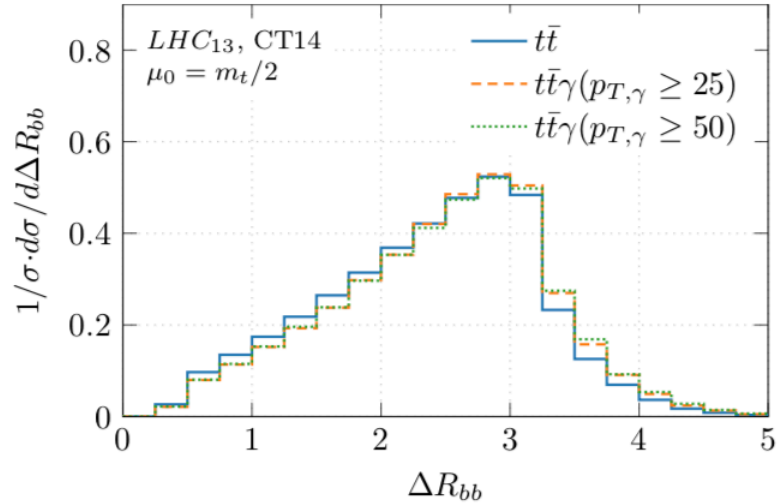
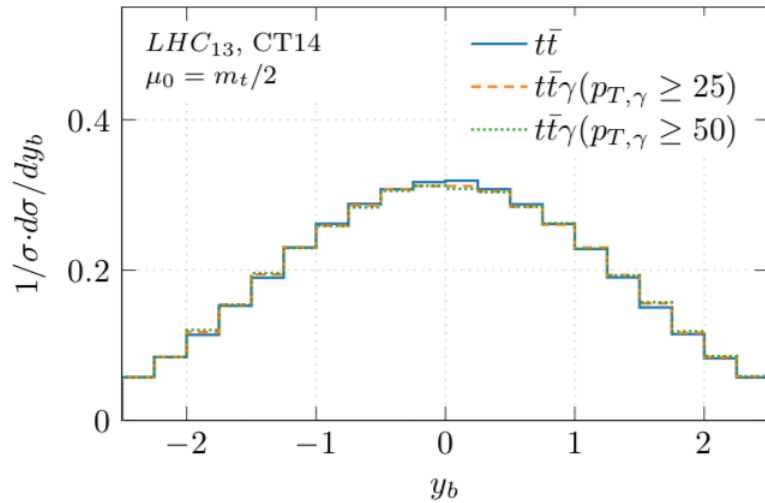
⌘ *Processes need to be correlated* → top quark pair production excellent candidate

$$\left( \frac{\mu_1}{\mu_0}, \frac{\mu_2}{\mu_0} \right) = \{(2, 2), (0.5, 0.5)\}$$

⌘ *Similar dynamical scale choice need to be implemented for  $\mu_1$  and  $\mu_2$  !*

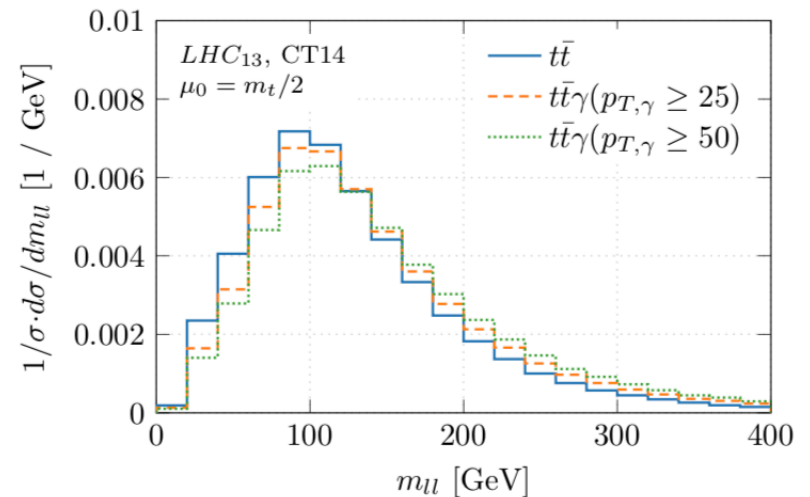
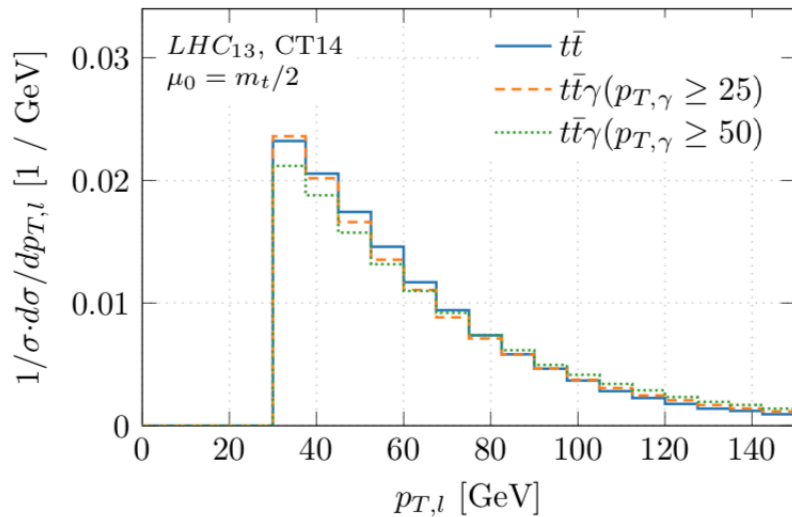
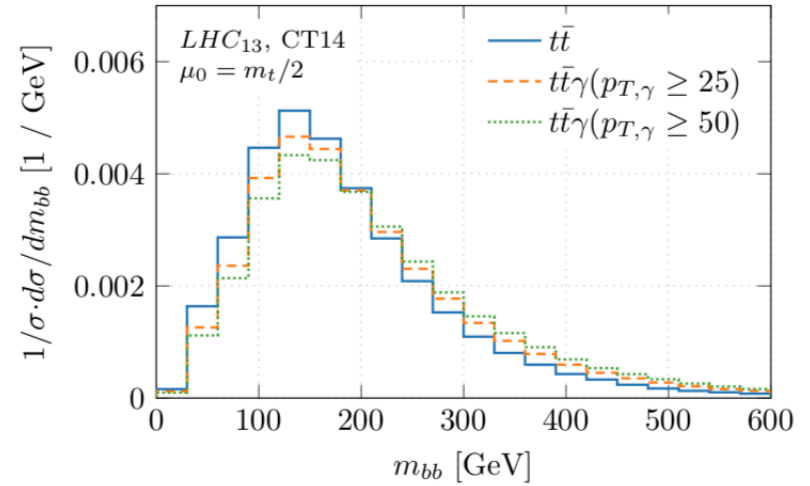
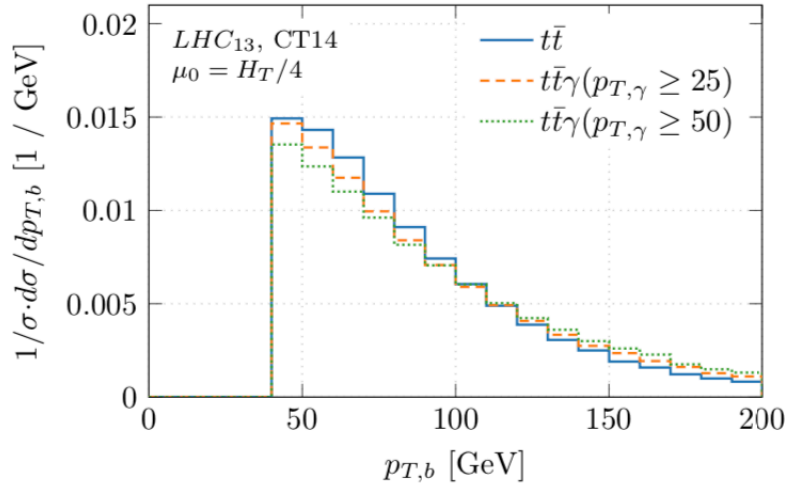
# $t\bar{t}\gamma$ & $t\bar{t}$

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}\gamma$  @ LHC<sub>13</sub>TeV



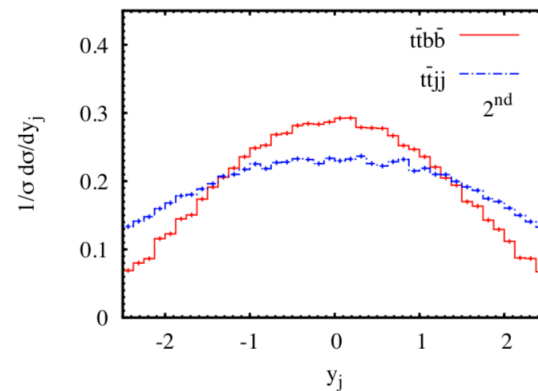
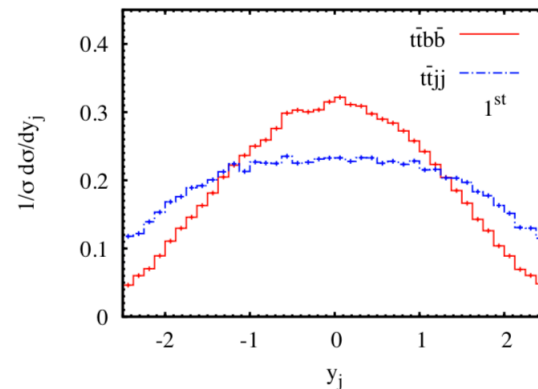
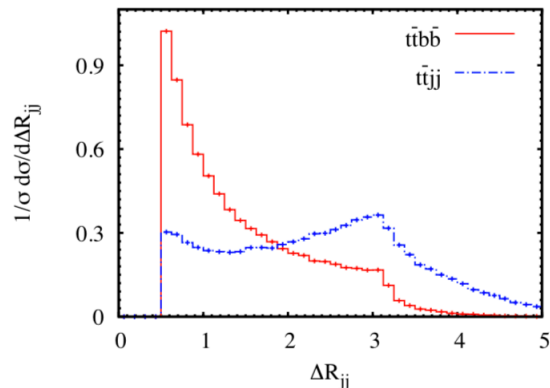
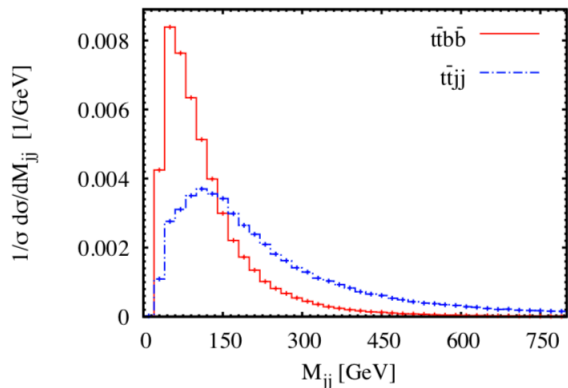
# $t\bar{t}\gamma$ & $t\bar{t}$

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}\gamma$  @ LHC<sub>13</sub>TeV



# ttbb & ttjj

$pp \rightarrow t\bar{t}b\bar{b} \text{ \& \ } t\bar{t}jj \text{ @ LHC}_{8\text{TeV}}$



- ⌘ Different jet kinematics makes the  $ttbb$  and  $ttjj$  processes uncorrelated in several observables
- ⌘ Scale uncertainty is not significantly reduced when taking ratio of cross sections

*On-shell Tops*

*LHC<sub>8TeV</sub>*

# tt $\gamma$ & tt

| PDF set, $\mu_R = \mu_F = \mu_0$ | $\sigma_{e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b}}^{\text{NLO}}$ [fb] | $\sigma_{e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b}\gamma}^{\text{NLO}}$ [fb]<br>$p_{T,\gamma} > 25$ GeV | $\sigma_{e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b}\gamma}^{\text{NLO}}$ [fb]<br>$p_{T,\gamma} > 50$ GeV |
|----------------------------------|--|---|---|
| CT14, $\mu_0 = m_t/2$            | 1629.4 <sup>+18.4 (1%)</sup> <sub>-144.7 (9%)</sub>              | 7.436 <sup>+0.074 (1%)</sup> <sub>-1.034 (14%)</sub>  | 3.081 <sup>+0.050 (2%)</sup> <sub>-0.514 (17%)</sub>  |
| CT14, $\mu_0 = H_T/4$            | 1620.5 <sup>+21.6 (1%)</sup> <sub>-118.8 (7%)</sub>              | 7.496 <sup>+0.099 (1%)</sup> <sub>-0.457 (6%)</sub>   | 3.125 <sup>+0.040 (1%)</sup> <sub>-0.142 (4%)</sub>   |
| MMHT14, $\mu_0 = m_t/2$          | 1650.5 <sup>+17.0 (1%)</sup> <sub>-152.7 (9%)</sub>              | 7.490 <sup>+0.080 (1%)</sup> <sub>-1.081 (14%)</sub>  | 3.093 <sup>+0.053 (2%)</sup> <sub>-0.535 (17%)</sub>  |
| NNPDF3.0, $\mu_0 = m_t/2$        | 1695.0 <sup>+18.4 (1%)</sup> <sub>-153.3 (9%)</sub>              | 7.718 <sup>+0.078 (1%)</sup> <sub>-1.102 (14%)</sub>  | 3.195 <sup>+0.054 (2%)</sup> <sub>-0.550 (17%)</sub>  |

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# $t\bar{t}\gamma/t\bar{t}$

$$\mathcal{R} = \frac{\sigma_{t\bar{t}\gamma}^{\text{NLO}}(\mu_1)}{\sigma_{t\bar{t}}^{\text{NLO}}(\mu_2)}$$

$$\mathcal{R}(\mu_0 = m_t/2, \text{CT14}, p_{T,\gamma} > 25 \text{ GeV}) = (4.56 \pm 0.25) \cdot 10^{-3} (5\%),$$

$$\mathcal{R}(\mu_0 = H_T/4, \text{CT14}, p_{T,\gamma} > 25 \text{ GeV}) = (4.62 \pm 0.06) \cdot 10^{-3} (1\%),$$

$$\mathcal{R}(\mu_0 = m_t/2, \text{CT14}, p_{T,\gamma} > 50 \text{ GeV}) = (1.89 \pm 0.16) \cdot 10^{-3} (8\%),$$

$$\mathcal{R}(\mu_0 = H_T/4, \text{CT14}, p_{T,\gamma} > 50 \text{ GeV}) = (1.93 \pm 0.06) \cdot 10^{-3} (3\%).$$

⌘ Our best NLO QCD predictions with dynamical scale choice:

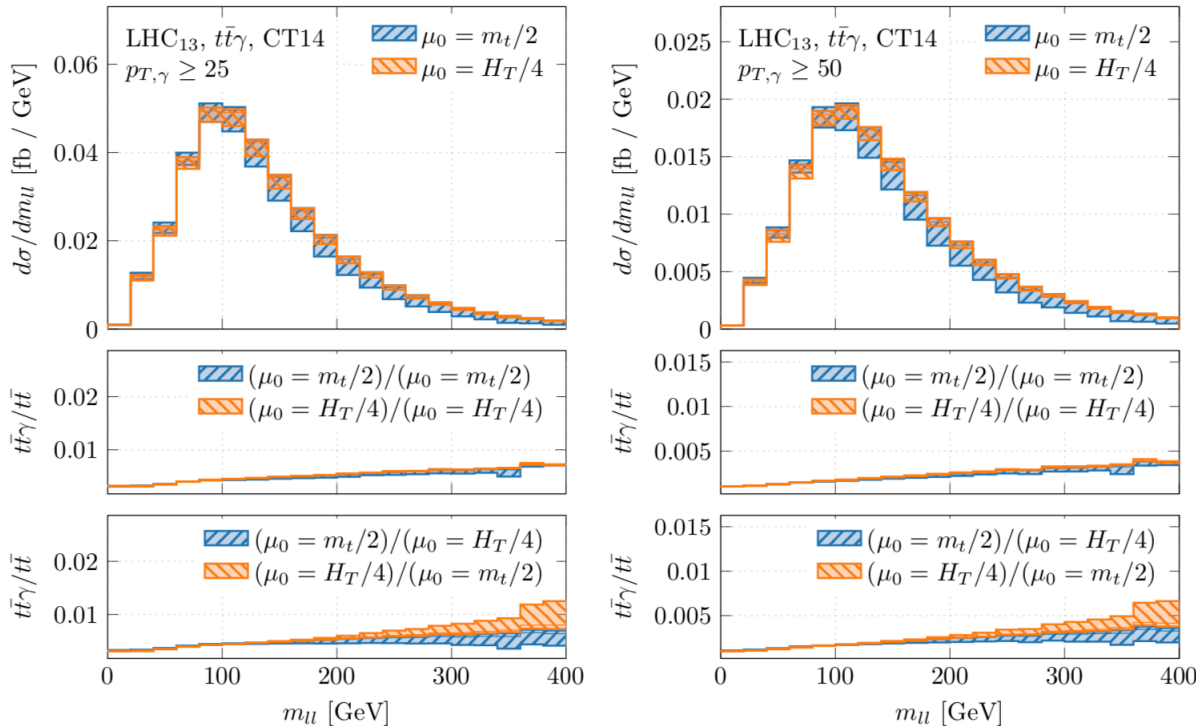
$$\mathcal{R}(\mu_0 = H_T/4, \text{CT14}, p_{T,\gamma} > 25 \text{ GeV}) = (4.62 \pm 0.06 [\text{scales}] \pm 0.02 [\text{PDFs}]) \cdot 10^{-3}$$

$$\mathcal{R}(\mu_0 = H_T/4, \text{CT14}, p_{T,\gamma} > 50 \text{ GeV}) = (1.93 \pm 0.06 [\text{scales}] \pm 0.02 [\text{PDFs}]) \cdot 10^{-3},$$



# Differential Cross Section Ratio

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$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma @ \text{LHC}_{13\text{TeV}}$

Theoretical uncertainties:

$\pm (1\% - 4\%)$   
*dynamical scale*

$\pm (20\% - 25\%)$   
*fixed scale*

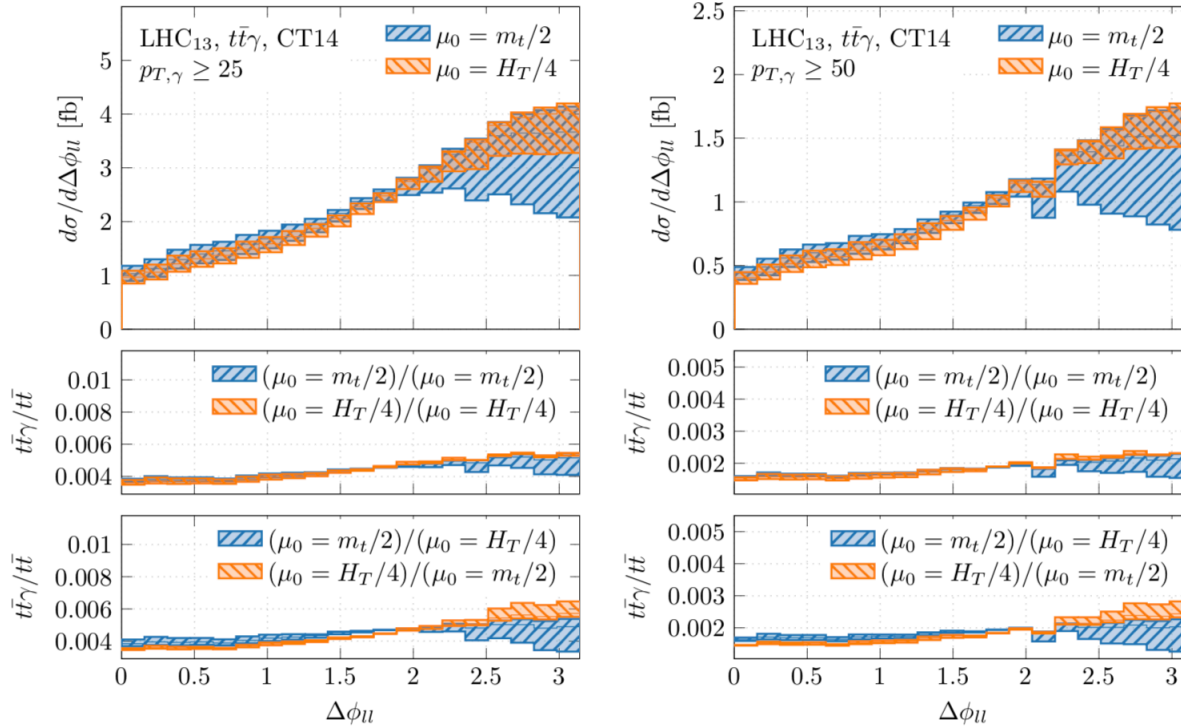
⌘ Should be compared to uncertainties for absolute differential cross section

❖ *up to  $\pm 10\%$  for  $\mu_0 = H_T/4$  & up to  $\pm 50\%$  for  $\mu_0 = m_t/2$*

⌘ When different scales are used in numerator and denominator *up to 60%*

# Differential Cross Section Ratio

*Bevilacqua, Hartanto, Kraus, Weber, Worek '18*



$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma @ \text{LHC}_{13\text{TeV}}$

Theoretical uncertainties:

$\pm (2\% - 3\%)$   
*dynamical scale*

$\pm (20\% - 30\%)$   
*fixed scale*

⌘ Should be compared to uncertainties for absolute differential cross section  
 ❖ *up to  $\pm 20\%$  for  $\mu_0 = H_T/4$  & up to  $\pm 50\%$  for  $\mu_0 = m_t/2$*

⌘ When different scales are used in numerator and denominator *up to 60%*

# Summary & Outlook

- ⌘ The most precise NLO QCD theoretical predictions for  $t\bar{t}\gamma$  in di-lepton channel
  - ❖ Complete off-shell effects for top quarks
  - ❖ Corrections to production & decays &  $t\bar{t}$  spin correlations
  - ❖ Possibility of using kinematic-dependent scales
- ⌘ NLO QCD corrections stable against  $p_{T,\gamma}$  &  $p_{T,b}$  cut
- ⌘ CT14 PDF uncertainties similar/smaller than difference between various PDF sets
- ⌘ Uncertainties due to scale dependence dominant source of theoretical systematics
- ⌘  $t\bar{t}\gamma$  relevant for BSM searches and studies of top quark properties
- ⌘ Cross section ratio(s) increase precision without going to NNLO QCD !
- ⌘ *Next steps:*
  - ❖ *Comparisons:* NWA vs. off-shell effects dedicated studies for  $t\bar{t}\gamma$
  - ❖ *Applications:* SM parameter extraction, disentangling and constraining anomalous couplings and more ...