



# QCD @ LHC - *Precision for Discoveries*

MALGORZATA WOREK



# Instead of Introduction

- Latest NLO & NNLO QCD results for  $2 \rightarrow 3$  &  $2 \rightarrow 5, 6 \dots$  processes in SM
  - Not only are they impressive, but there are plenty of them
- Tell story, hopefully interesting one about precision in top-quark physics
  - A few results for SM top-quark associated processes
    - ✓  $pp \rightarrow tt + \gamma$
    - ✓  $pp \rightarrow tt + Z$  ( $Z \rightarrow \nu\nu$ )
    - ✓  $pp \rightarrow tt + H$
  - Top-quark results in the context of BSM physics
    - ✓  $pp \rightarrow tt + \text{Dark Matter}$
    - ✓  $pp \rightarrow tt + H \Leftrightarrow \mathcal{CP}$  structure of top-quark Yukawa interaction
- **MY GOAL:**
  - Identify which effects are important & should be taken into account
  - Top-quark production and decays with complete off-shell effects included @ NLO QCD
  - HELAC-NLO & Fixed order calculations @ LHC 13 TeV



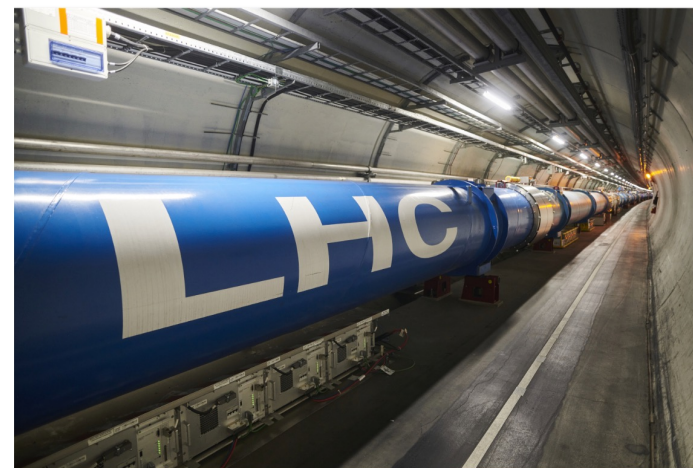
# Instead of Introduction

- **SM** ⇨ Extremely fun, exciting, enjoyable time for people working on SM ⇨ **QCD + EW**
- **BSM** ⇨ Significant number of open questions remains  
Search for new phenomena key aspect of LHC
- **BSM DIRECT SEARCHES**
  - Many proposals for New Physics
  - No model of New Physics really stands out
  - No obvious candidates to look for @ LHC
  - $tt$ ,  $tt + jets$ ,  $tt + V$  ⇨ Important backgrounds for BSM
- **BSM INDIRECT SEARCHES**
  - New Physics as small corrections to SM reactions
  - *Precision SM measurements @ LHC*
    - ✓ Run 3 & High Luminosity LHC, ...
  - *High Precision Theoretical Predictions for SM Processes*
    - ✓ Top Quark

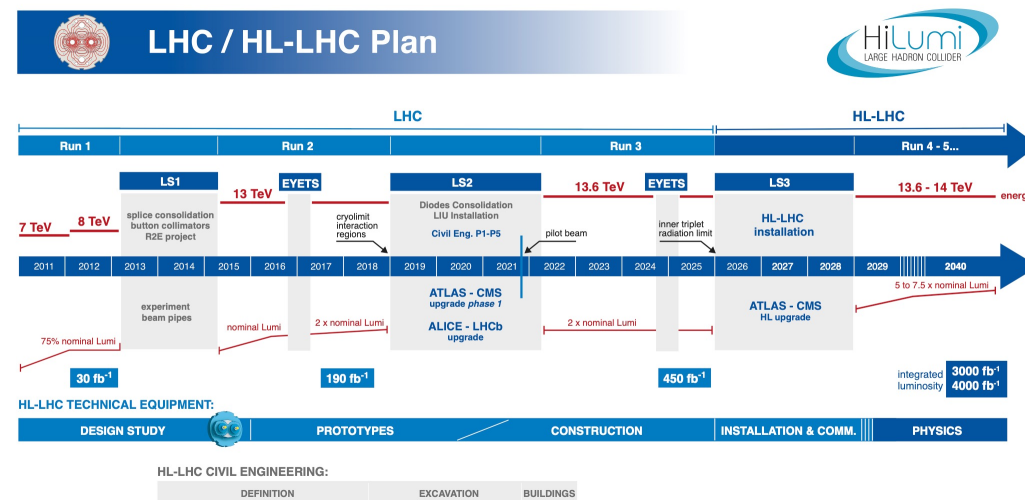
## Large Hadron Collider restarts

Beams of protons are again circulating around the collider's 27-kilometre ring, marking the end of a multiple-year hiatus for upgrade work

22 APRIL, 2022



The LHC tunnel at point 1 (Image: CERN)



CERN: LHC/HL-LHC Plan (last update February 2022)

# Why Top Quark is so Special

- HEAVIEST OBSERVED PARTICLE

$$m_t = (173.34 \pm 0.76) \text{ GeV}$$

World Combination '14  
ATLAS, CDF, CMS, D0

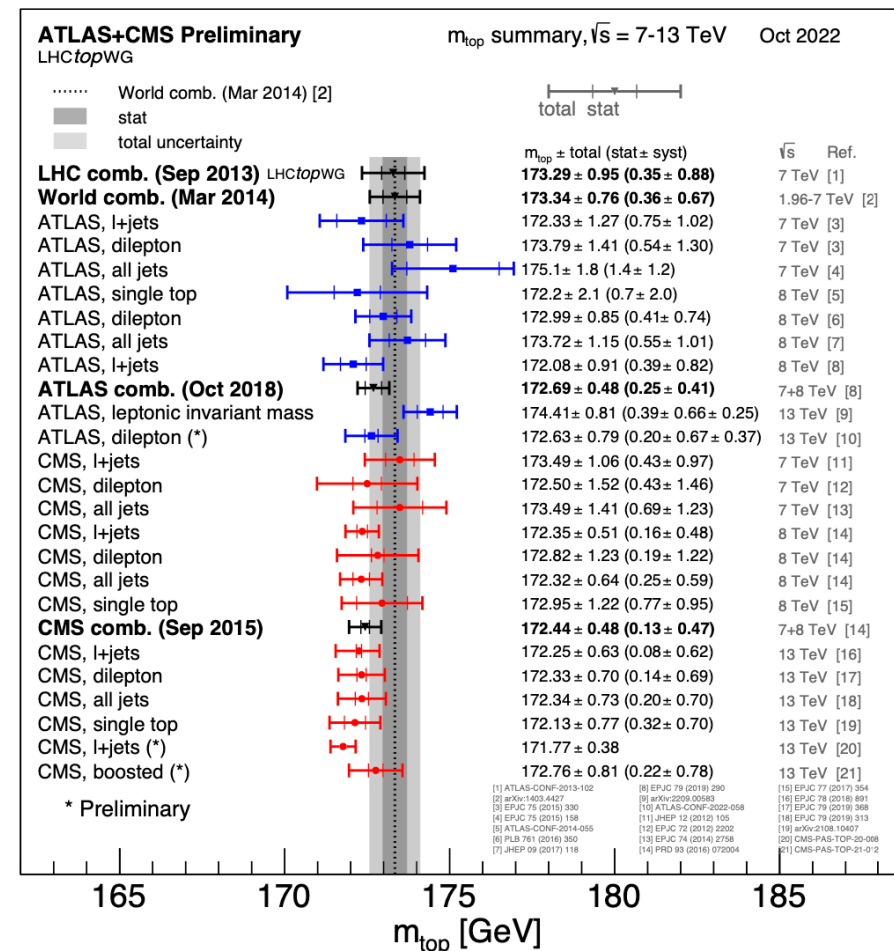
- Substantial Yukawa coupling

$$Y_t = \sqrt{2} m_t / v \approx 1$$

- Special relation with SM Higgs boson
- Short lifetime  $\Rightarrow$  Decay before bound states can be formed
- Direct handle on top-quark properties from its decay products

$$b\text{-jets, light jets, } l^\pm, p_T^{\text{miss}}$$

- FINAL STATES THAT ARE PRESENT IN ALMOST ALL BSM SCENARIOS

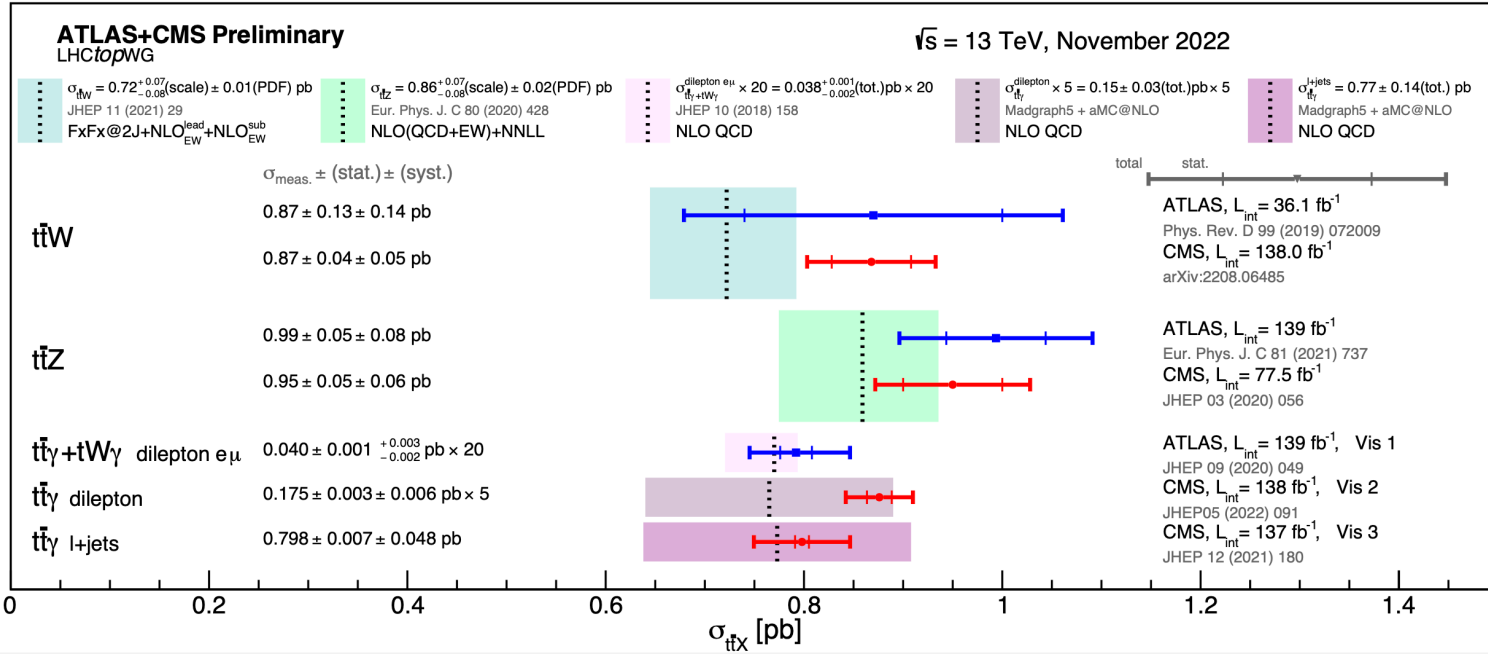


$$m_t = (171.77 \pm 0.38) \text{ GeV}$$

CMS Collaboration '22



# Associated $t\bar{t}$ Production

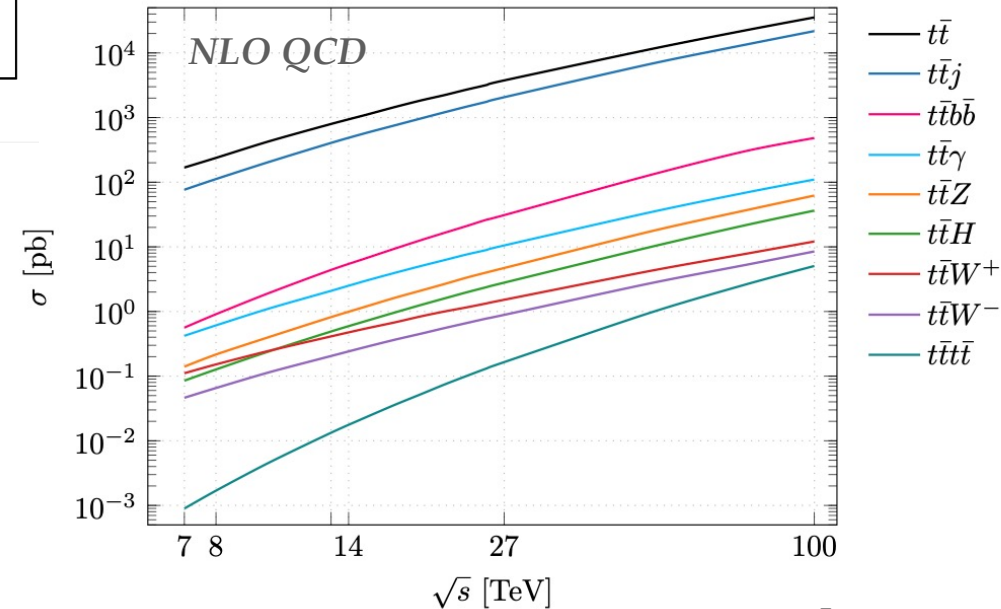


Summary of ATLAS and CMS measurements of  $pp \rightarrow t\bar{t} + X$ ,  $X = \gamma, Z, W$  cross sections at 13 TeV

MORE EXCLUSIVE FINAL STATES ARE PRODUCED @ LHC

Report of the Topical Group on Top quark physics and heavy flavor production for Snowmass 2021  
e-Print: 2209.11267 [hep-ph]

Total cross sections for various  $pp \rightarrow t\bar{t} + X$  processes as function of center-of-mass energy  
Also shown is  $pp \rightarrow t\bar{t}$



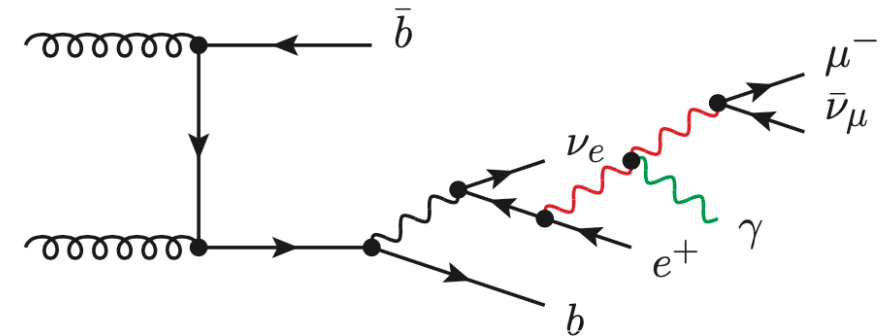
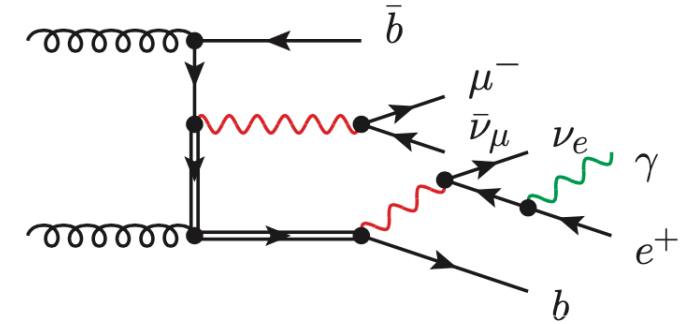
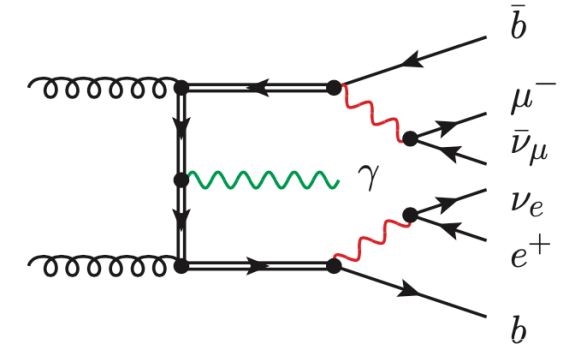
# Full Off-Shell Effects

- Off-shell top quarks & W described by Breit-Wigner propagators
- Double-, single- & non-resonant top-quark & W contributions included
- All interference effects incorporated at matrix element level
- NLO QCD corrections to  $t\bar{t}\gamma$  production & top-quark decays
- Nonfactorizable NLO QCD corrections included
- Cross-talk between production & both top-quark decays
- Photon emission in production & top-quark decays
- NLO spin correlations

Bevilacqua, Hartanto, Kraus, Weber, Worek '18 '19 '20

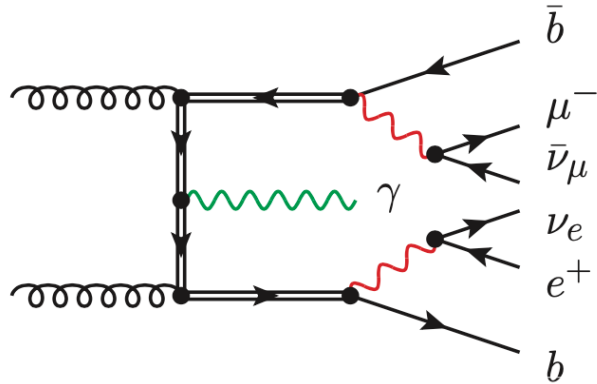
NLO  $t\bar{t}\gamma$

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma + X$$



# Narrow Width Approximation

- Full NWA  $\Leftrightarrow$  NWA<sub>Full</sub>

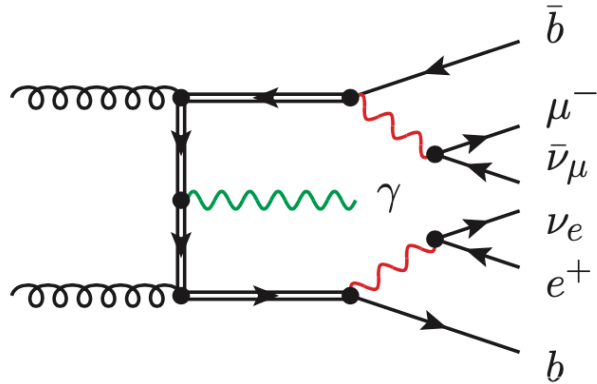


- Works in the limit  $\Leftrightarrow \Gamma/m \rightarrow 0$
- Incorporates only double resonant contributions
- Restricts unstable tops & W to on-shell states
- NLO QCD correction separately to  $t\bar{t}\gamma$  production & separately to both top-quark decays
- NLO QCD nonfactorizable corrections missing
- No cross-talk between production & both top-quark decays
- NLO spin correlations

# Narrow Width Approximation

NLO  $t\bar{t}\gamma$

- Full NWA  $\Leftrightarrow$  NWA<sub>Full</sub>



- Works in the limit  $\Leftrightarrow \Gamma/m \rightarrow 0$
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- NLO QCD correction separately to  $t\bar{t}\gamma$  production & both top-quark decays
- NLO QCD nonfactorizable corrections missing
- No cross-talk between production & both top-quark decays
- NLO spin correlations

- NWA with LO Decays  $\Leftrightarrow$  NWA<sub>LOdec</sub>

- Without NLO QCD corrections to top-quark decays
- Photons only in production
- LO spin correlations

$$pp \rightarrow t\bar{t}\gamma \rightarrow W^+W^- b\bar{b}\gamma \rightarrow e^+\nu_e \mu^-\bar{\nu}_\mu b\bar{b}\gamma + X$$

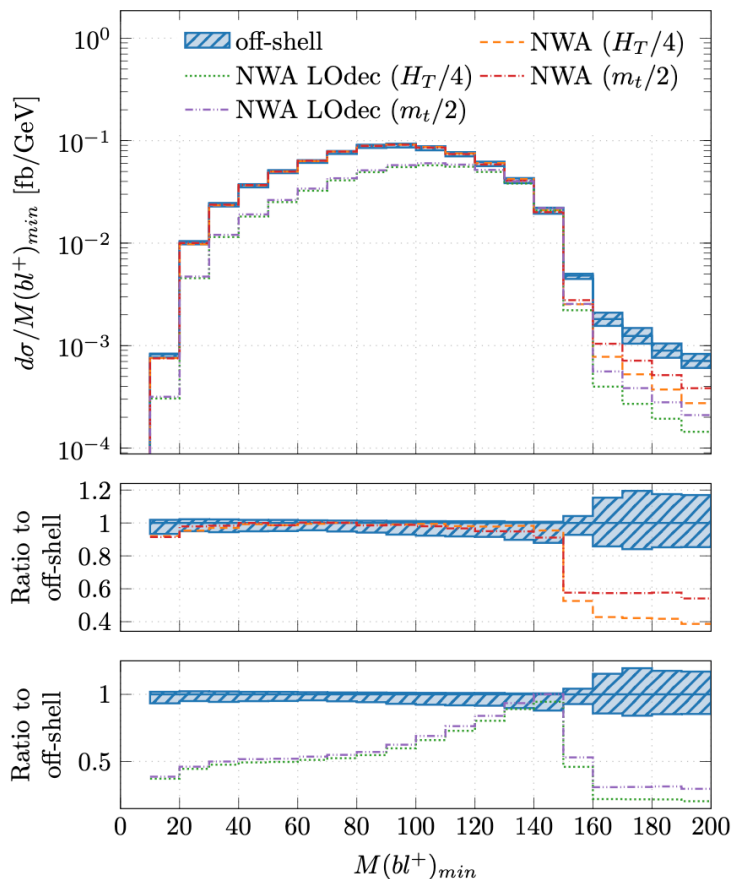
$$\Gamma_t = 1.35159 \text{ GeV}, m_t = 173.2 \text{ GeV}, \Gamma_t/m_t \approx 0.008$$

$$\frac{\Gamma_W}{m_W} > \frac{\Gamma_t}{m_t} \gg \frac{\Gamma_H}{m_H},$$

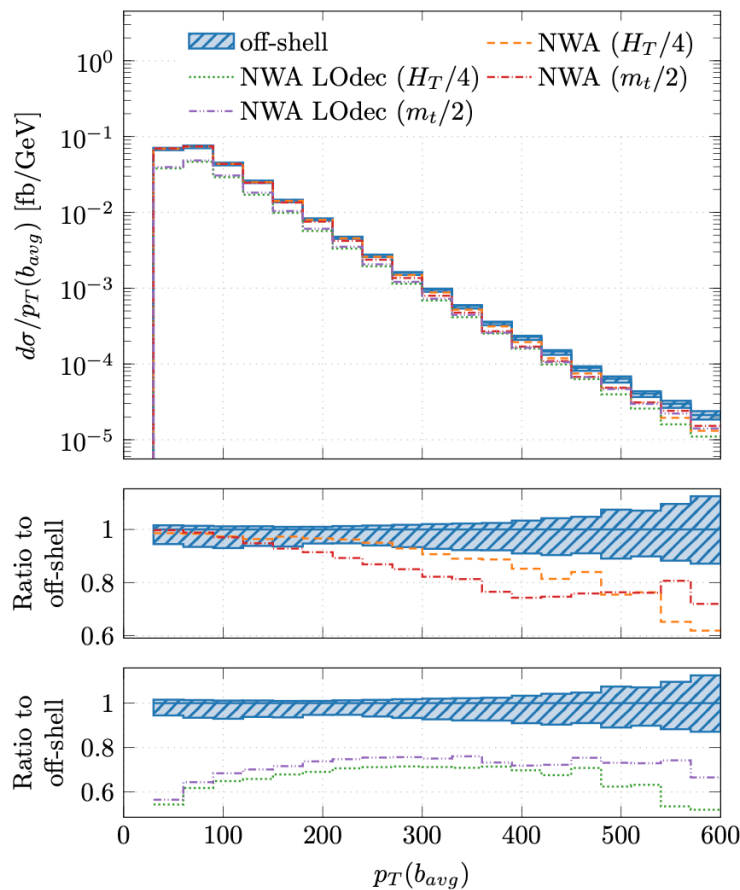
$$2.6\% > 0.8\% \gg 0.003\%.$$

# How Good is NWA

$$M(bl^+) = \sqrt{m_t^2 - m_W^2} \approx 153 \text{ GeV}$$



Bevilacqua, Hartanto, Kraus, Weber, Worek '18 '19 '20



$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma + X$$

## Dimensionful observables

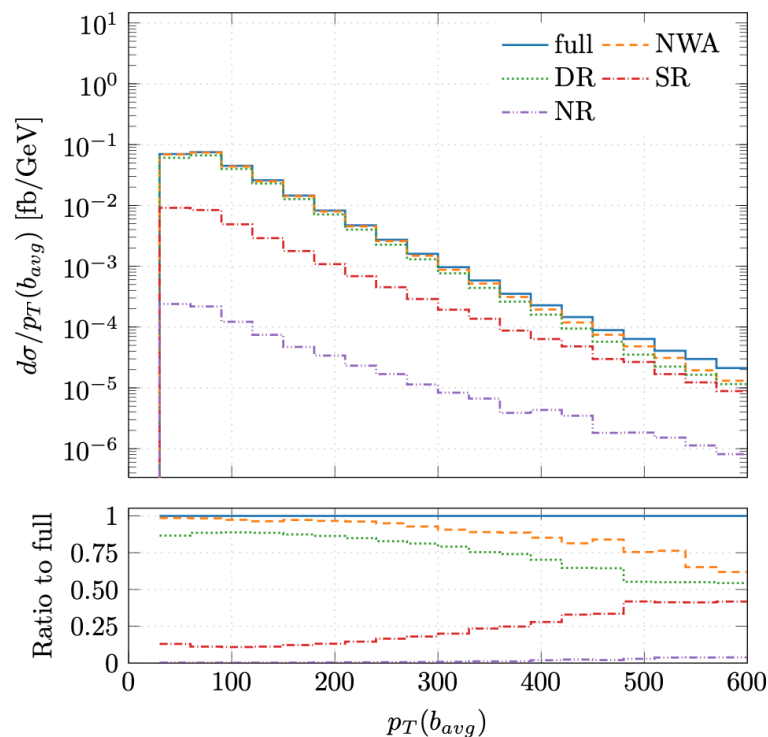
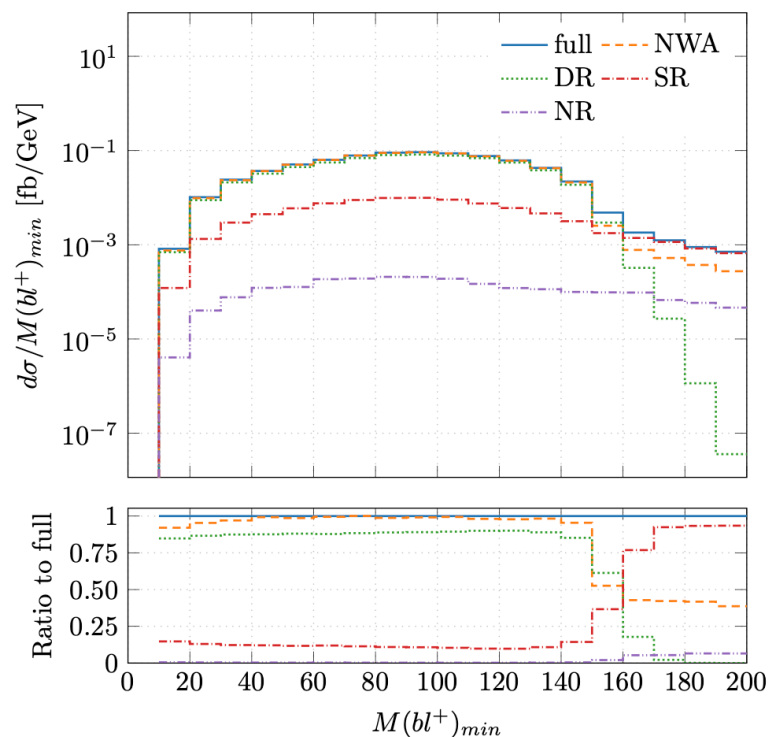
- Sensitive to non-factorizable top quark corrections *50% - 60%*
- Sensitive phase-space regions
  - *Kinematical edges*
  - *High  $p_T$  regions*
- NLO QCD corrections to top-quark decays *12% - 17%*

*Normalisation & shape differences due to not adequate renormalisation & factorisation scale setting*



# Various Phase-Space Regions

Bevilacqua, Hartanto, Kraus, Weber, Worek '18 '19 '20



$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma + X$$

## Dimensionful observables

- Sensitive to non-factorizable top quark corrections
- Effects up to *50% – 60%*
- Sensitive phase-space regions
  - *Kinematical edges*
  - *High  $p_T$  regions*

*Normalisation & shape differences due to large single top-quark contributions and interference effects*

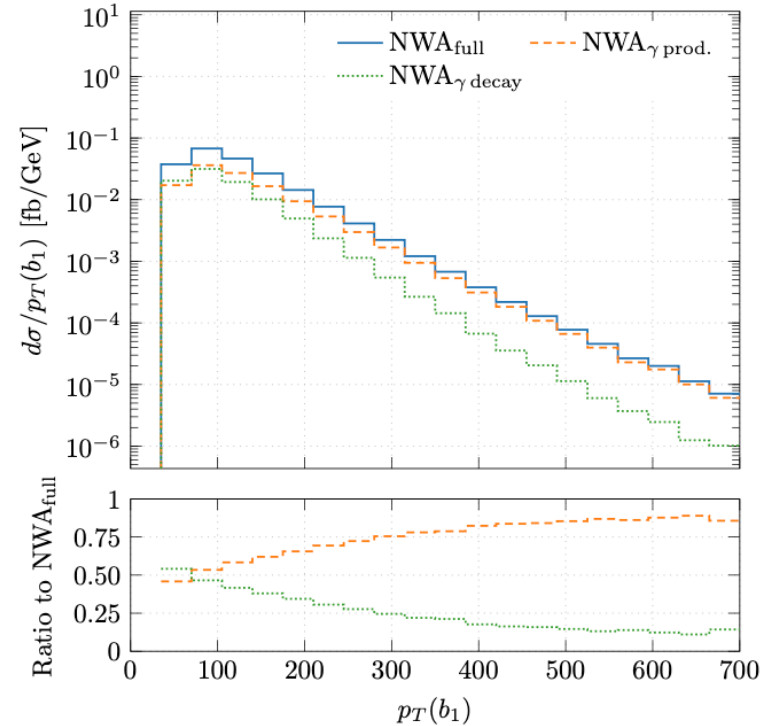
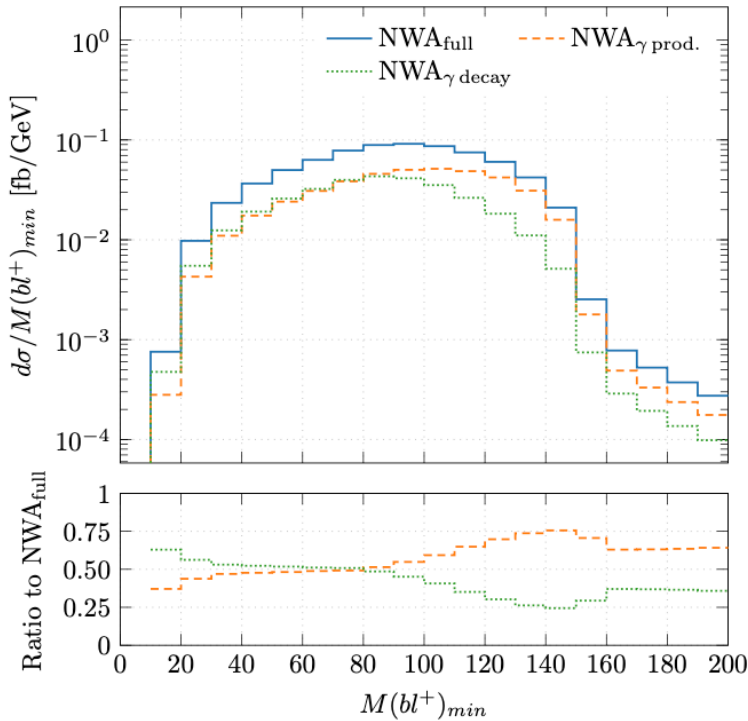
Not due to new physics effects

# $\gamma$ in Top-Quark Production & Decays

NLO  $t\bar{t}\gamma$

Bevilacqua, Hartanto, Kraus, Weber, Worek '18 '19 '20

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma + X$$



*Normalisation & shape differences due to large  $\gamma$  emission contributions in top-quark decays*

Not due to new physics effects

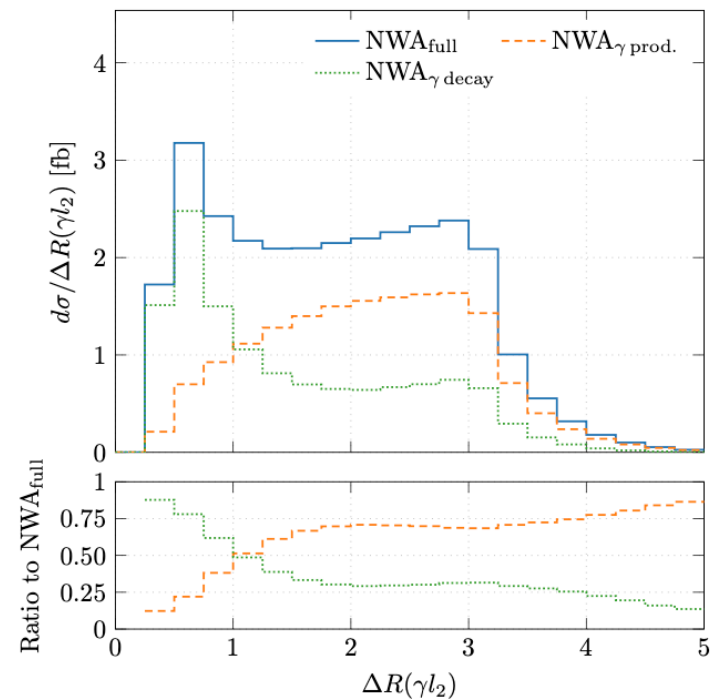
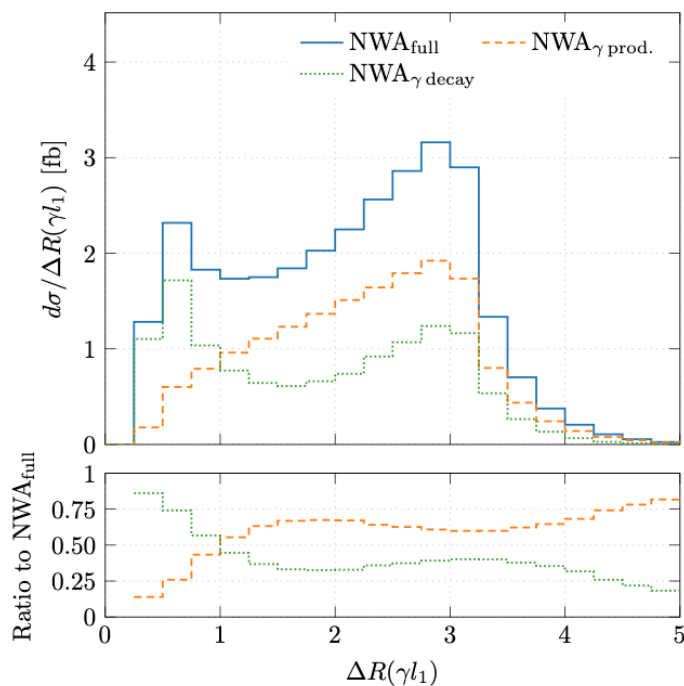
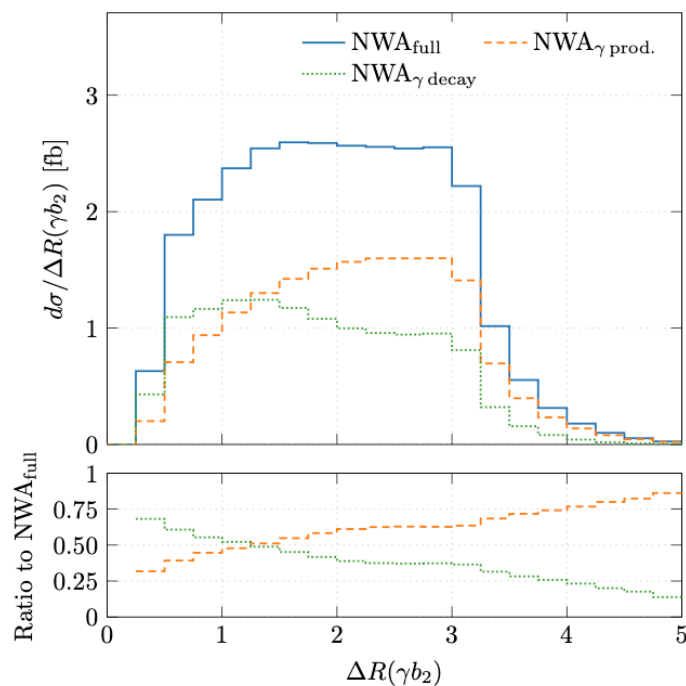
- For  $p_{T,b} > 40 \text{ GeV}$ 
  - 57%  $\Rightarrow \gamma$  in production
  - 43%  $\Rightarrow \gamma$  in top-quark decays
- For  $p_{T,b} > 25 \text{ GeV}$ 
  - $\gamma$  in top-quark decays increases up to almost 50%
- Photon radiation is distributed evenly between  $t\bar{t}\gamma$  production & top-quark decays

# $\gamma$ in Top-Quark Production & Decays

NLO  $t\bar{t}$

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma + X$$

Bevilacqua, Hartanto, Kraus, Weber, Worek '18 '19 '20



Normalisation & shape differences due to  $\gamma$  emission contributions in top-quark decays

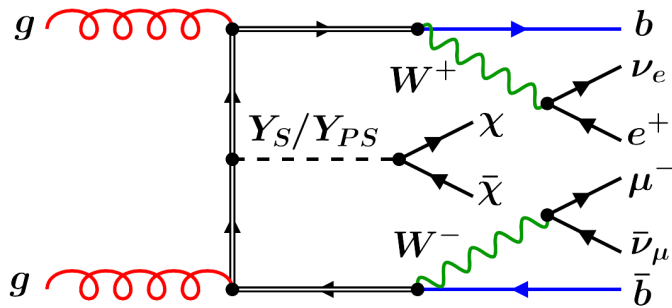
Not due to new physics effects

# Associated $t\bar{t}$ + Dark Matter Production

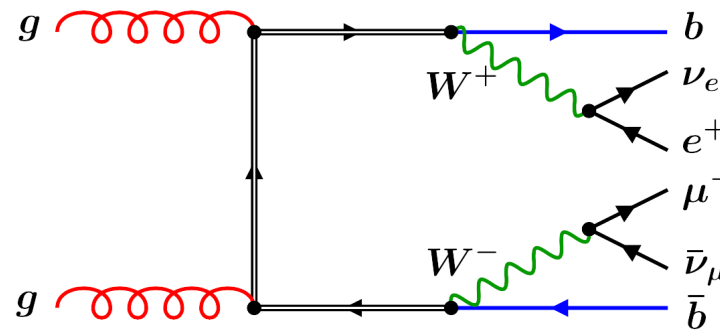
- $t\bar{t}$  + DM  $\Leftrightarrow$  Top-quark backgrounds:  $t\bar{t}$  &  $t\bar{t}Z$

Haisch, Pani, Polesello '17

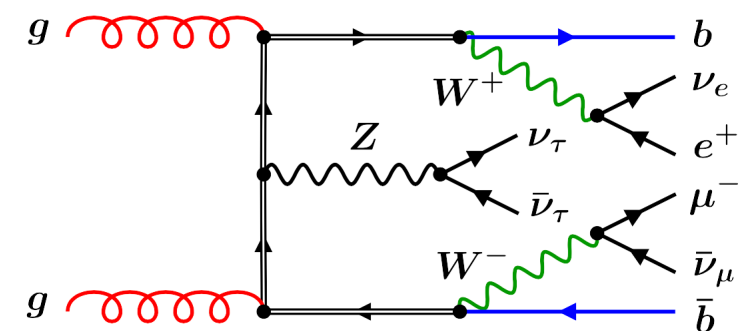
$$pp \rightarrow t\bar{t} + Y_{S/PS} \rightarrow W^+W^-b\bar{b} + Y_{S/PS} \rightarrow e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b} + \chi\chi$$



SIGNAL



LARGEST BACKGROUND



IRREDUCIBLE BACKGROUND

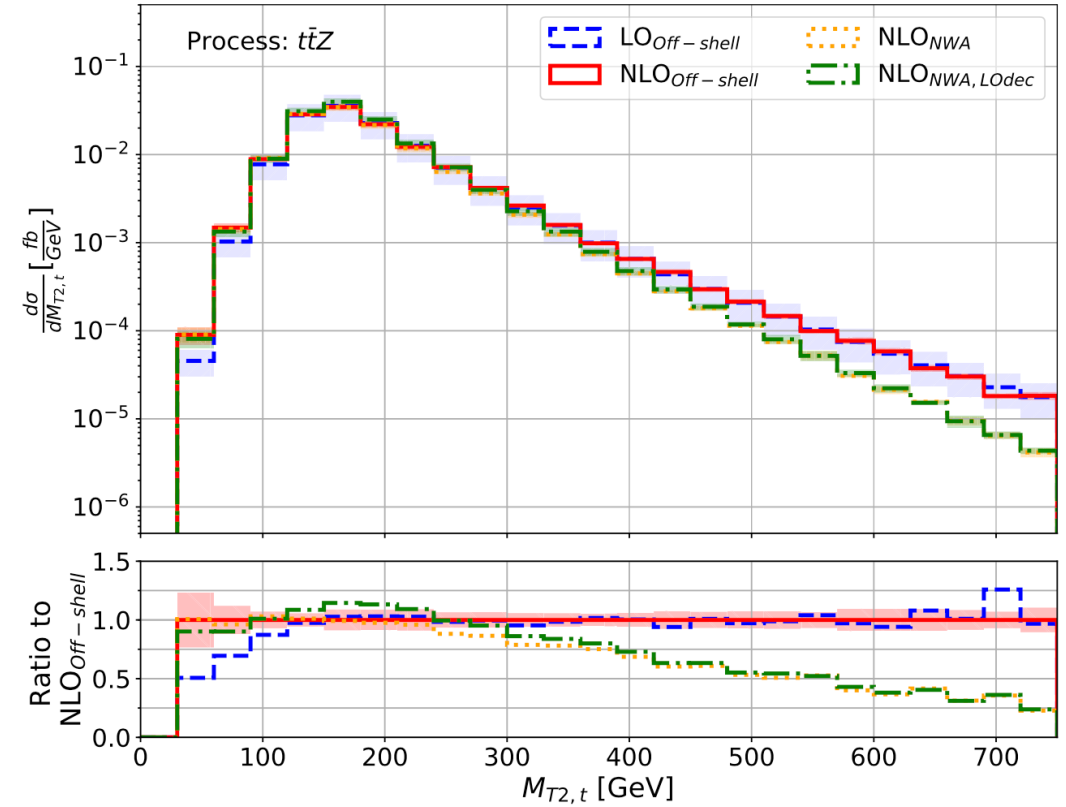
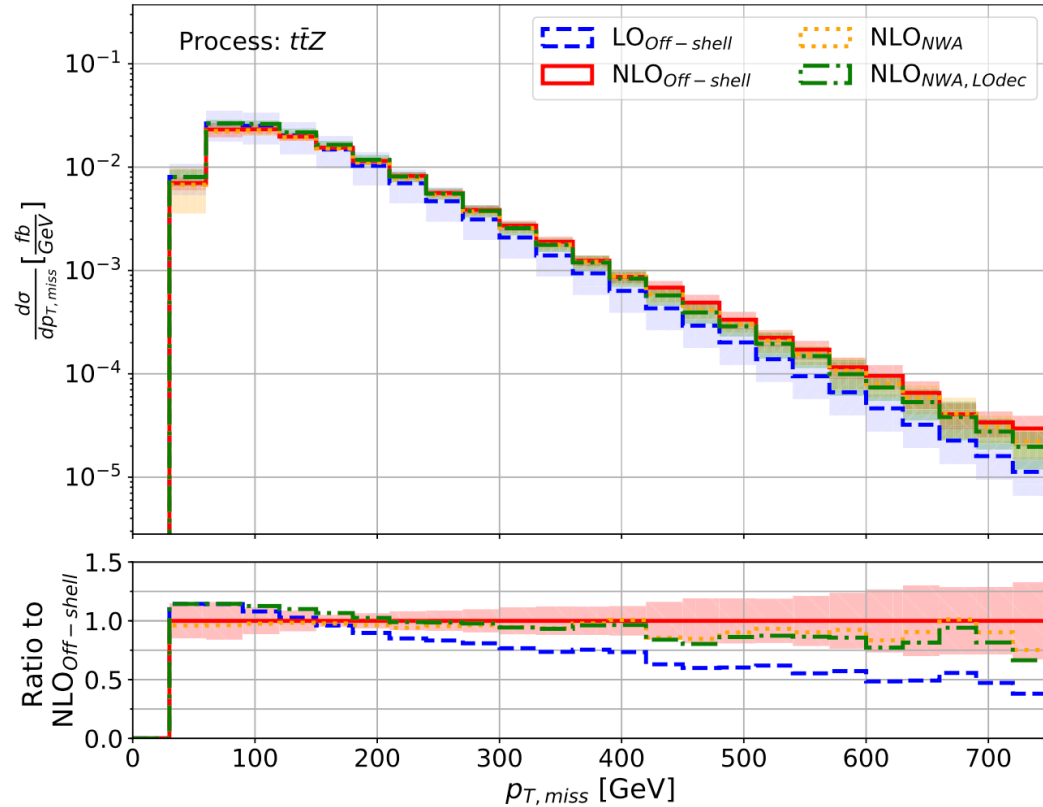
- SIMPLIFIED SPIN-0 S-CHANNEL MEDIATOR MODEL**  $\Leftrightarrow$  Fermionic DM particle  $\chi$  & mediator  $Y$  that can either be a scalar  $Y_S$  or pseudoscalar  $Y_{PS}$
- FINAL STATES**  $\Leftrightarrow$   $2l^\pm$ ,  $2b$ -jets, large  $p_T^{miss}$
- OBSERVABLE**  $\Leftrightarrow$   $M_{T2,W}$  &  $M_{T2,t}$  &  $p_T^{miss}$   $\Leftrightarrow$  Observables with kinematical edges & high  $p_T$  regions

# Associated $tt + Z$ Production

NLO  $ttZ$

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} \nu_\tau \bar{\nu}_\tau + X$$

Hermann, Worek '21



Comparison of differential distributions for  $ttZ$  background process for different modelling approaches



# *tt & tt + Z Production After Exclusive Cuts*

Hermann, Worek '21

Process	Order	Scale	$\sigma_{\text{uncut}}$ [fb]	$\sigma_{\text{cut}}$ [fb]	$\sigma_{\text{cut}}/\sigma_{\text{uncut}}$ (%)	Events for $L = 300 \text{ fb}^{-1}$
$t\bar{t}$ NWA	LO	$H_T/4$	1061	0	0.0	0
	LO	$E_T/4$	984	0	0.0	0
	LO	$m_t$	854	0	0.0	0
	NLO	$H_T/4$	1097	0	0.0	0
	NLO, LO dec	$H_T/4$	1271	0	0.0	0
$t\bar{t}Z$ NWA	LO	$H_T/3$	0.1223	0.0130	11	47
	LO	$E_T/3$	0.1052	0.0116	11	42
	LO	$m_t + m_Z/2$	0.1094	0.0134	12	48
	NLO	$H_T/3$	0.1226	0.0130	11	47
	NLO, LO dec	$H_T/3$	0.1364	0.0140	10	50
$t\bar{t}$ Off-shell	LO	$H_T/4$	1067	0.0144	0.0013	17
	LO	$E_T/4$	989	0.0131	0.0013	16
	LO	$m_t$	861	0.0150	0.0017	18
	NLO	$H_T/4$	1101	0.0156	0.0014	19
$t\bar{t}Z$ Off-shell	LO	$H_T/3$	0.1262	0.0135	11	49
	LO	$E_T/3$	0.1042	0.0115	11	41
	LO	$m_t + m_Z/2$	0.1135	0.0140	12	50
	NLO	$H_T/3$	0.1269	0.0134	11	48

**tt & ttZ**

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} + X$$

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \nu_\tau \bar{\nu}_\tau + X$$

*Before & after applying additional cuts*

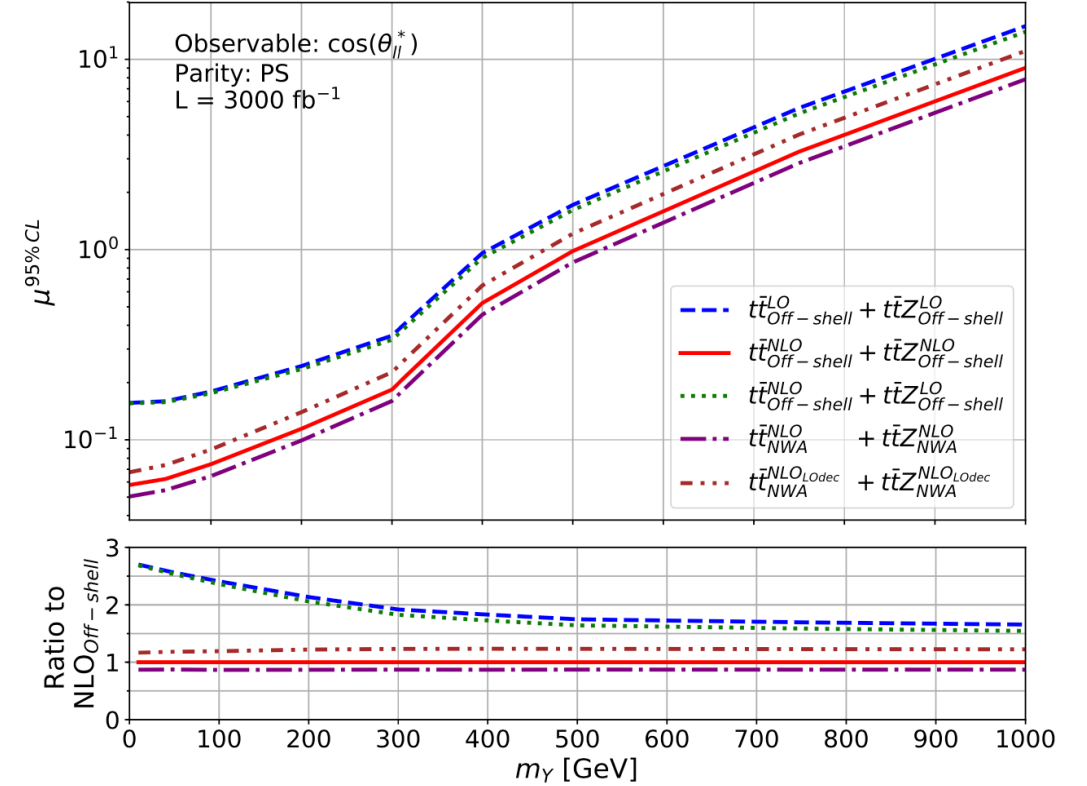
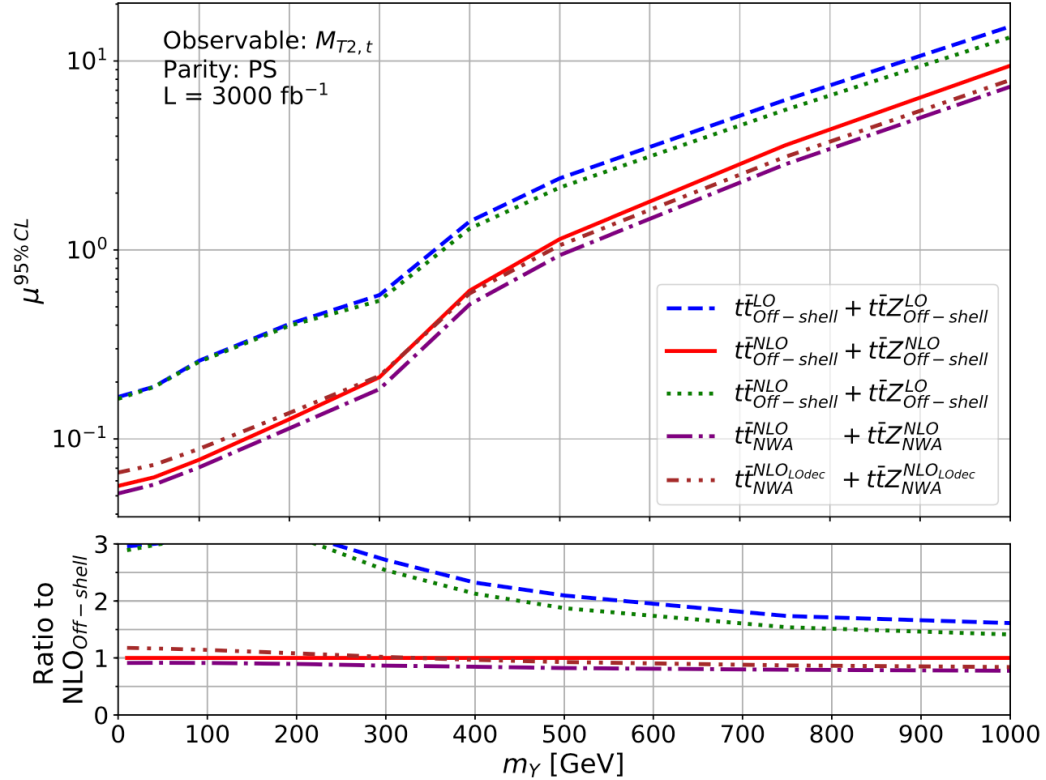
- After cuts **25%** of events come from *tt*
- **NLO** smaller uncertainties w.r.t LO, NLO + LO decays

Comparison of LO and NLO integrated cross sections for two background processes in NWA and including full off-shell effects before and after applying additional cuts

Lepton flavour factors are included: *4 for tt & 12 for ttZ*

# BSM Exclusion Limits

Comparison of signal strength exclusion limits computed with different background predictions for pseudoscalar mediator scenario



$$M_{T2,t}^2 = \min_{\substack{\mathbf{p}_T^{\nu_1} + \mathbf{p}_T^{\nu_2} \\ = \mathbf{p}_{T,\text{miss}}} } [\max\{M_T^2(\mathbf{p}_T^{(lb)_1}, \mathbf{p}_T^{\nu_1}),$$

$$M_T^2(\mathbf{p}_T^{(lb)_2}, \mathbf{p}_T^{\nu_2})\}]$$

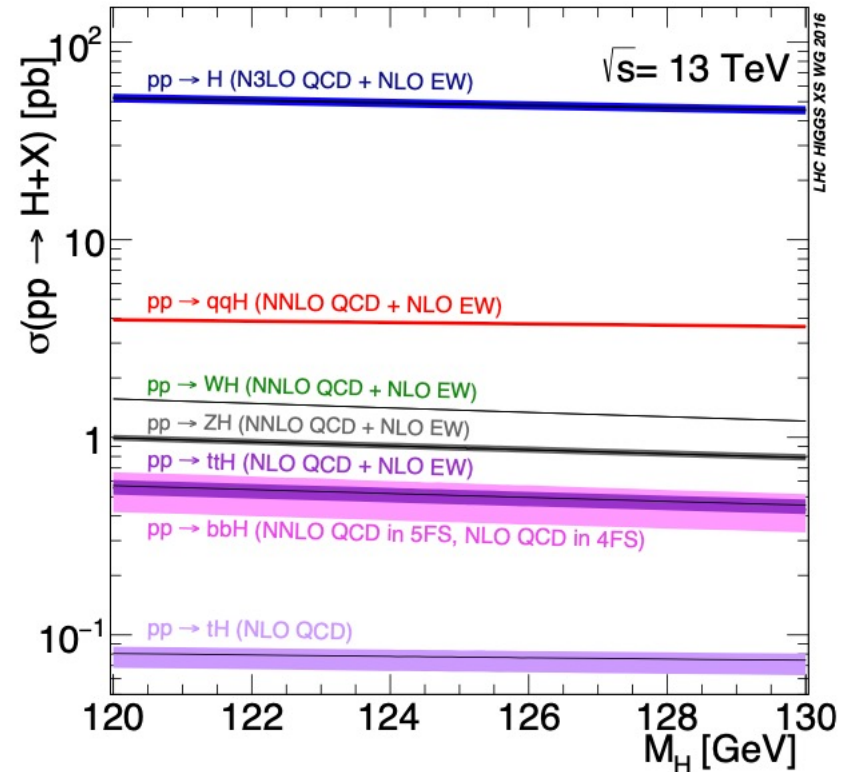
$$\cos(\theta_{ll}^*) = \tanh(|\eta_{l_1} - \eta_{l_2}|/2)$$

$$M_T^2(\mathbf{p}_T^{(lb)_i}, \mathbf{p}_T^{\nu_i}) = M_{(lb)_i}^2 + 2(E_T^{(lb)_i} E_T^{\nu_i} - \mathbf{p}_T^{(lb)_i} \cdot \mathbf{p}_T^{\nu_i})$$

# Associated $tt + H$ Production

- Allows for direct probe of Yukawa interaction and it's  $CP$  nature at tree level  $\Rightarrow$  In SM Higgs is  $CP$  even
- Higgs  $CP$  studies in  $ttH$  are ongoing
- ATLAS ATLAS Collaboration arXiv:2004.04545 [hep-ex]
  - Purely  $CP$ -odd hypothesis excluded  $3.9\sigma$
  - $CP$ -mixing angle  $|\alpha_{CP}| > 43^\circ$  excluded at 95% CL
- CMS CMS Collaboration arXiv:2208.02686 [hep-ex]
  - Purely  $CP$ -odd hypothesis  $|f^{Htt}_{CP}| = 1$  excluded  $3.7\sigma$
  - $CP$ -mixing angle  $|f^{Htt}_{CP}| < 0.55$  at 68 % CL
- Weak constrains exist on possible admixture between  $CP$ -even &  $CP$ -odd component
- DEVIATION FROM SM VALUE WOULD INDICATE NEW PHYSICS EFFECTS

SM Higgs boson production cross section at 13 TeV



$pp \rightarrow ttH$  only 1% of total  $pp \rightarrow H + X$

Report of the LHC Higgs Cross Section Working Group  
arXiv:1610.07922 [hep-ph]

# Associated $t\bar{t} + H$ Production

- $CP$ -even,  $CP$ -odd &  $CP$ -mixed Higgs boson in Higgs characterisation framework

$$\mathcal{L}_{t\bar{t}H} = -\bar{\psi}_t \frac{Y_t}{\sqrt{2}} \left( \underbrace{\kappa_{Ht\bar{t}} \cos(\alpha_{CP})}_{CP\text{-even}} + i \underbrace{\kappa_{Att\bar{t}} \sin(\alpha_{CP}) \gamma_5}_{CP\text{-odd}} \right) \psi_t H$$

Mixing angle

---


$$\mathcal{L}_{HVV} = \kappa_{HVV} \left( \frac{1}{2} g_{HZZ} Z_\mu Z^\mu + g_{HWW} W_\mu^+ W^{-\mu} \right) H$$

Scenario	$\alpha$
Purely $CP$ -even	$0^\circ$ or $180^\circ$
Purely $CP$ -odd	$90^\circ$
Mixed	$\neq 0^\circ, \neq 90^\circ, \neq 180^\circ$

Recover SM results for any value of  $\alpha_{CP}$  & ensure consistency with bounds from GF and VBF

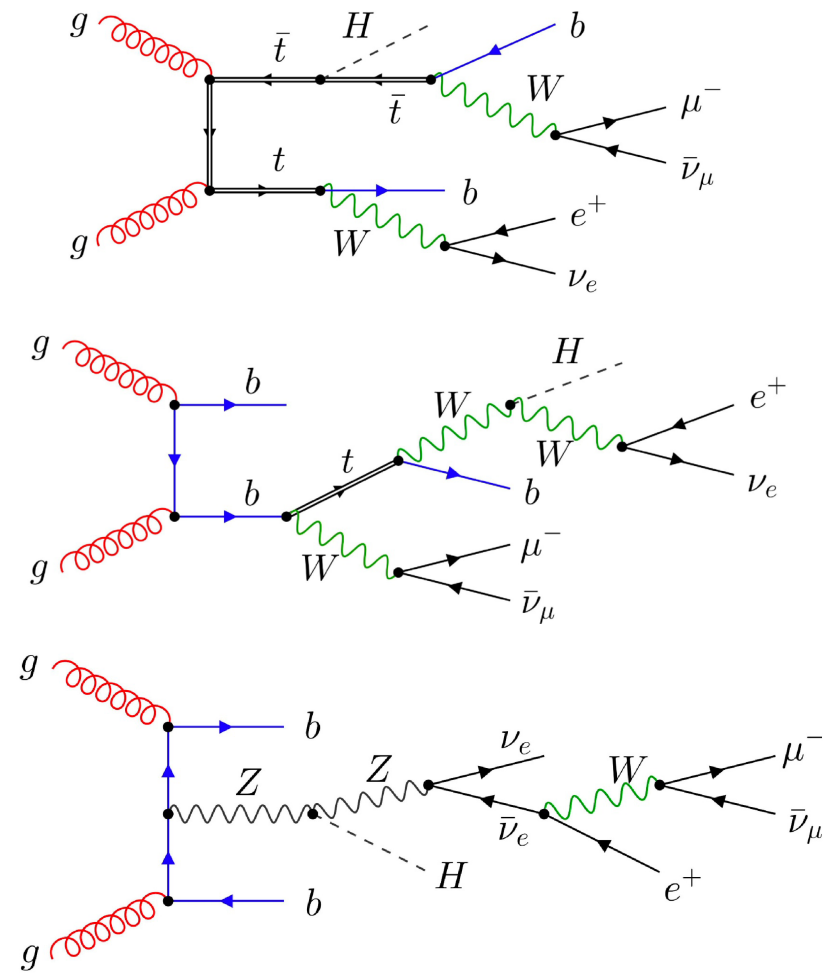
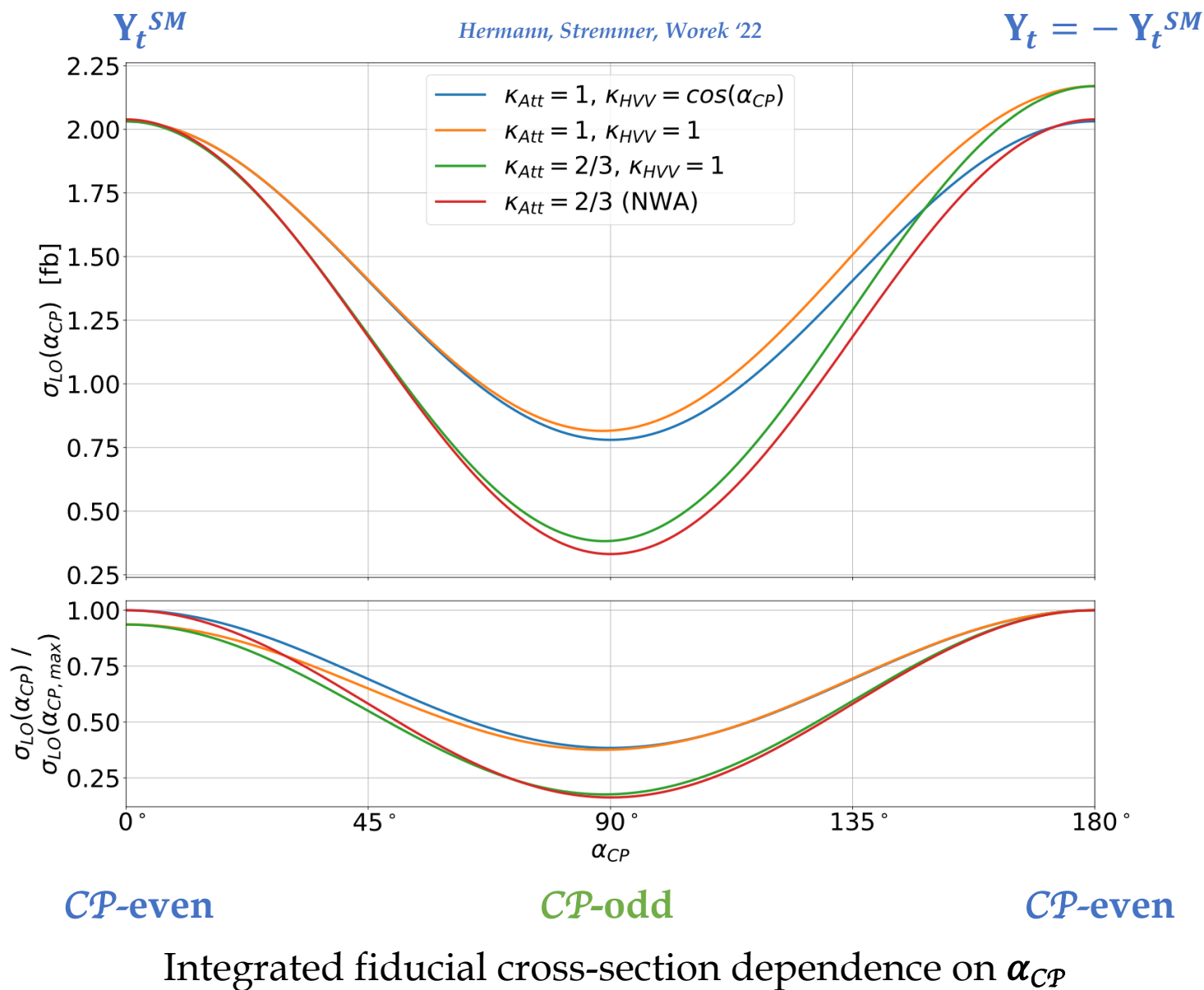
$$\kappa_{Att\bar{t}} = 2/3 \text{ and } \kappa_{Ht\bar{t}} = 1$$

$$\kappa_{HVV} = 1$$

Artoisenet, Aquino, Demartin, Frederix, Frixione, Maltoni, Mandal, Mathews, Mawatari, Ravindran, Seth, Torrielli, Zaro '13  
 Maltoni, Mawatari, Zaro '14  
 Demartin, Maltoni, Mawatari, Page, Zaro '14  
 Demartin, Maltoni, Mawatari, Zaro '15  
 Demartin, Maier, Maltoni, Mawatari, Zaro '17

- Extended Higgs sector:  $\kappa_{Att\bar{t}} = 1$      $\kappa_{HVV} = \cos(\alpha_{CP})$ 
  - Same coupling for scalar and pseudoscalar Higgs
  - Relevant for SM extensions like 2HDM

# Associated $tt + H$ Production



- **NWA** is symmetric  $\alpha_{CP} \rightarrow \pi - \alpha_{CP}$
- *Off-shell contributions break symmetry*
- Full result is only symmetric for  $\kappa_{HVV} = \cos(\alpha_{CP})$



# Associated $tt + H$ Production

NLO  $ttH$

Hermann, Stremmer, Worek '22

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} H + X$$

$\alpha_{CP}$		Off-shell	NWA	Off-shell effects	
<b>CP-even</b>	0 (SM)	$\sigma_{LO}$ [fb]	2.0313(2) <sup>+0.6275 (31%)</sup> <sub>-0.4471 (22%)</sub>	2.0388(2) <sup>+0.6290 (31%)</sup> <sub>-0.4483 (22%)</sub>	-0.37%
		$\sigma_{NLO}$ [fb]	2.466(2) <sup>+0.027 (1.1%)</sup> <sub>-0.112 (4.5%)</sub>	2.475(1) <sup>+0.027 (1.1%)</sup> <sub>-0.113 (4.6%)</sub>	-0.36%
		$\sigma_{NLO_{LOdec}}$ [fb]	—	2.592(1) <sup>+0.161 (6.2%)</sup> <sub>-0.242 (9.3%)</sub>	
		$\mathcal{K} = \sigma_{NLO}/\sigma_{LO}$	1.21	1.21 (LOdec: 1.27)	
<b>CP-mixed</b>	$\pi/4$	$\sigma_{LO}$ [fb]	1.1930(2) <sup>+0.3742 (31%)</sup> <sub>-0.2656 (22%)</sub>	1.1851(1) <sup>+0.3707 (31%)</sup> <sub>-0.2633 (22%)</sub>	0.66%
		$\sigma_{NLO}$ [fb]	1.465(2) <sup>+0.016 (1.1%)</sup> <sub>-0.071 (4.8%)</sub>	1.452(1) <sup>+0.015 (1.0%)</sup> <sub>-0.069 (4.8%)</sub>	0.89%
		$\sigma_{NLO_{LOdec}}$ [fb]	—	1.517(1) <sup>+0.097 (6.4%)</sup> <sub>-0.144 (9.5%)</sub>	
		$\mathcal{K} = \sigma_{NLO}/\sigma_{LO}$	1.23	1.23 (LOdec: 1.28)	
<b>CP-odd</b>	$\pi/2$	$\sigma_{LO}$ [fb]	0.38277(6) <sup>+0.13123 (34%)</sup> <sub>-0.09121 (24%)</sub>	0.33148(3) <sup>+0.11240 (34%)</sup> <sub>-0.07835 (24%)</sub>	13.4%
		$\sigma_{NLO}$ [fb]	0.5018(3) <sup>+0.0083 (1.2%)</sup> <sub>-0.0337 (6.7%)</sub>	0.4301(2) <sup>+0.0035 (0.8%)</sup> <sub>-0.0264 (6.1%)</sub>	14.3%
		$\sigma_{NLO_{LOdec}}$ [fb]	—	0.4433(2) <sup>+0.0323 (7.3%)</sup> <sub>-0.0470 (11%)</sub>	
		$\mathcal{K} = \sigma_{NLO}/\sigma_{LO}$	1.31	1.30 (LOdec: 1.34)	

## NLO CORRECTIONS:

- 21% - 31% corrections
- Increase with mixing angle
- Reduced scale uncertainties
- NLO with LO decays overestimates NLO results by few percent

## OFF-SHELL EFFECTS:

- Small for **CP-even** and **CP-mixed** Higgs boson
- Large effects for **CP-odd** Higgs boson

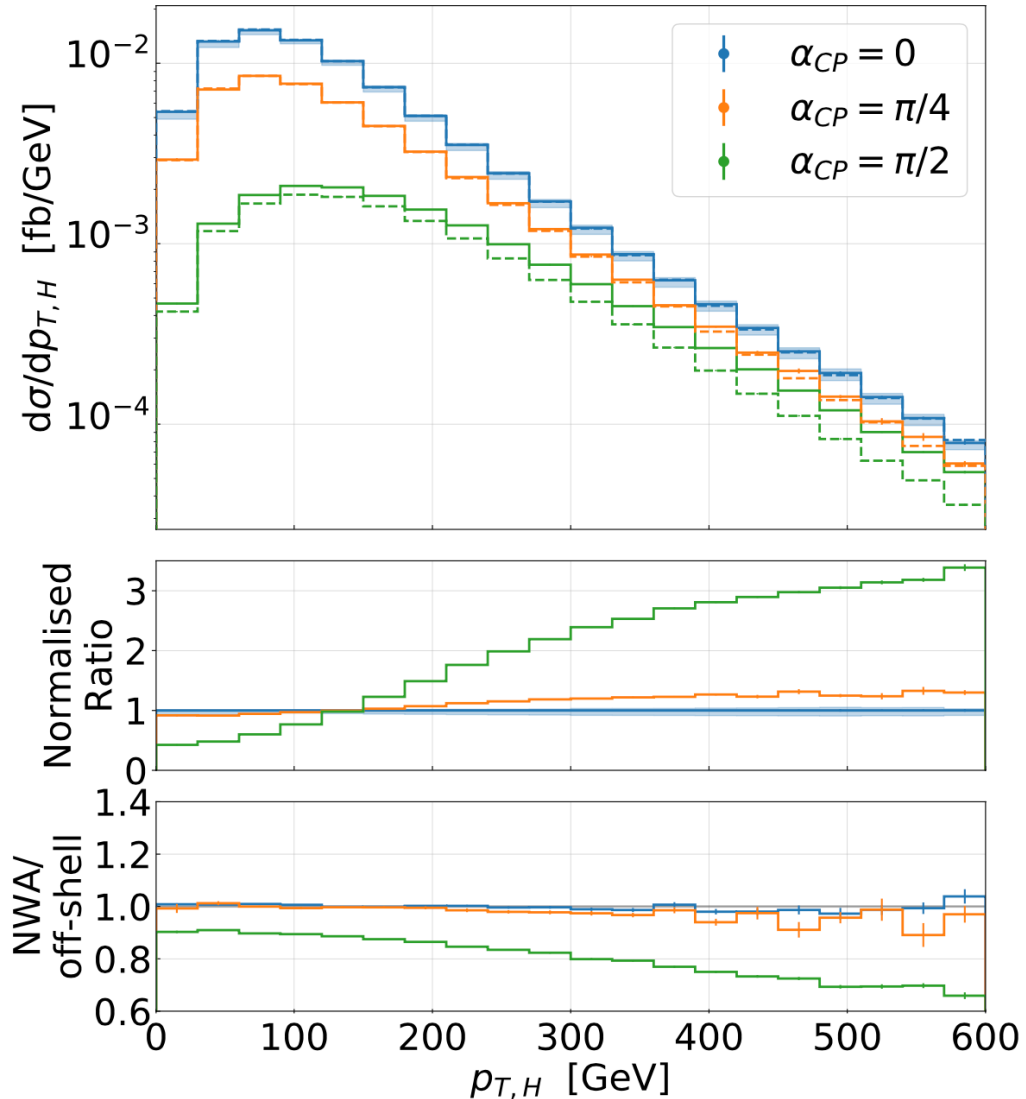
Comparison of LO and NLO QCD integrated fiducial cross-sections as calculated in NWA, NWA with LO top-quark decays and full off-shell approach

# Associated $tt + H$ Production

NLO  $ttH$

Hermann, Stremmer, Worek '22

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} H + X$$



## SHAPE COMPARISON:

- $\mathcal{CP}$ -even and  $\mathcal{CP}$ -mixed similar, small difference in tails
- Tails much more pronounced in  $\mathcal{CP}$ -odd case even up to 200%

## OFF-SHELL EFFECTS:

- Large effects on size and shape for  $\mathcal{CP}$ -odd Higgs boson
- Up to 35% effects driven by single-resonant top-quark contributions
- Only a few % effects for  $\mathcal{CP}$ -even and  $\mathcal{CP}$ -mixed

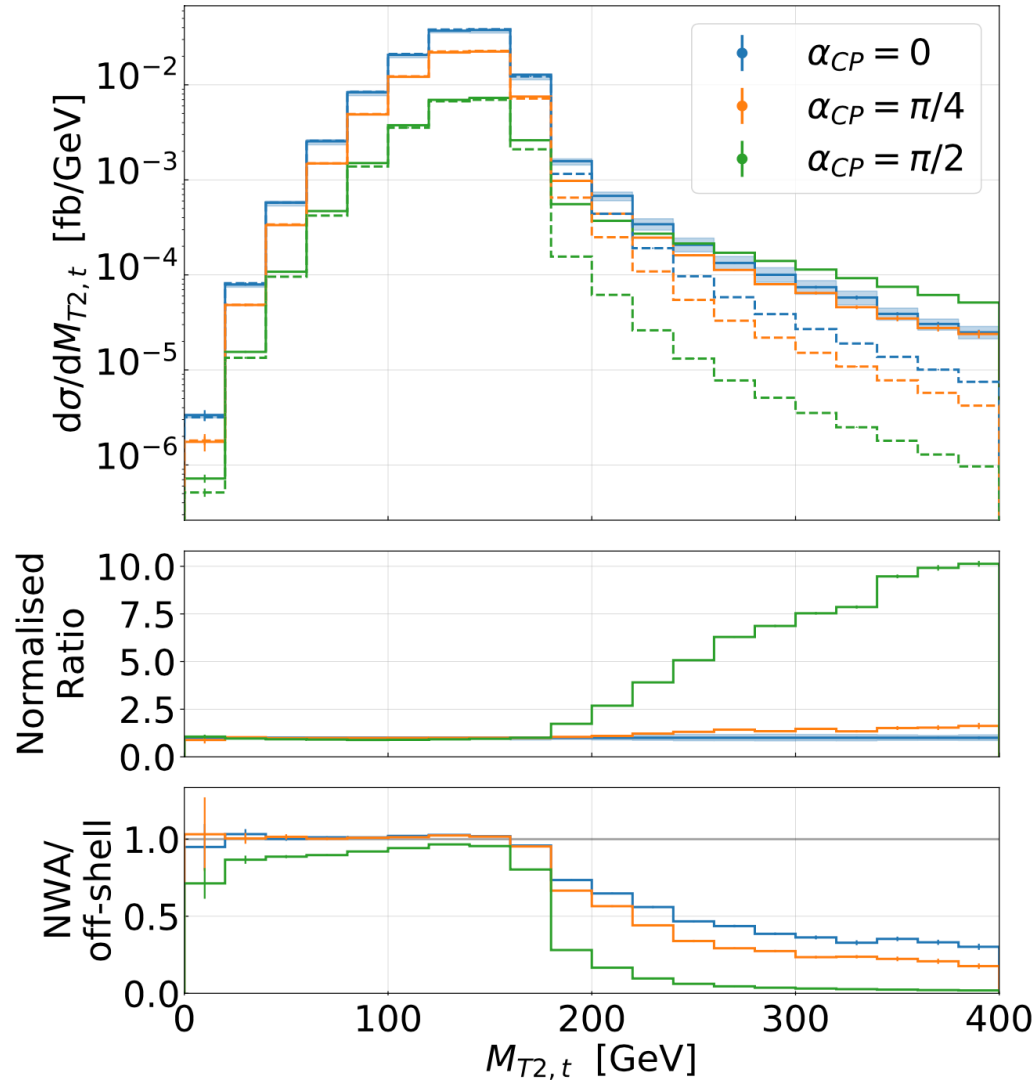
Off-shell Results: Solid line  
NWA Results: Dashed line

# Associated $tt + H$ Production

NLO  $ttH$

Hermann, Stremmer, Worek '22

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} H + X$$



## SHAPE COMPARISON:

- **CP-even** and **CP-mixed** rather similar for small values
- Large difference above kinematic edges  $M_{T2,t} > m_t$
- Can reach factor of 10
- 
- For **CP-odd** case cross-section is actually the largest

## OFF-SHELL EFFECTS:

- Large effects **70% - 99%** for all **CP-states** for  $M_{T2,t} > m_t$
- Driven by single-resonant top-quark contributions
- Largest effects for **CP-odd** Higgs boson

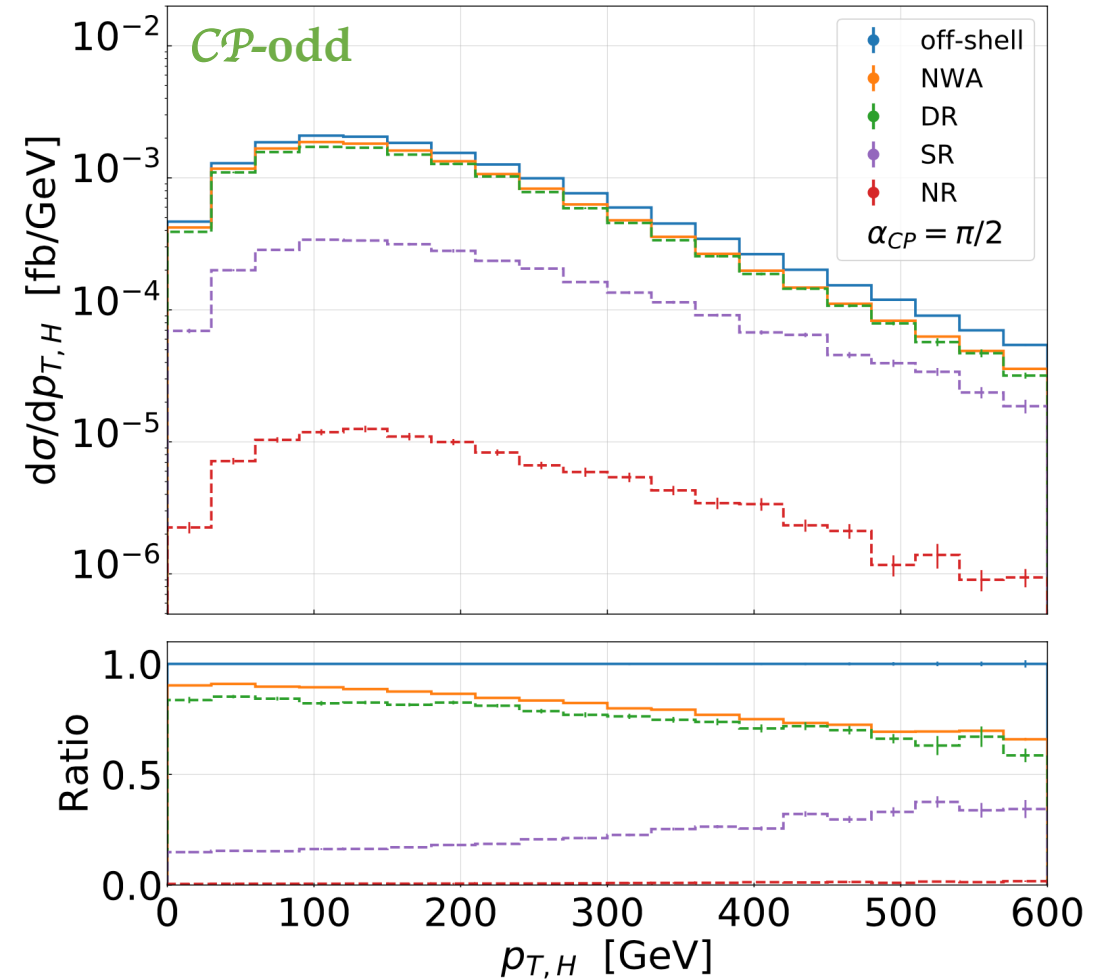
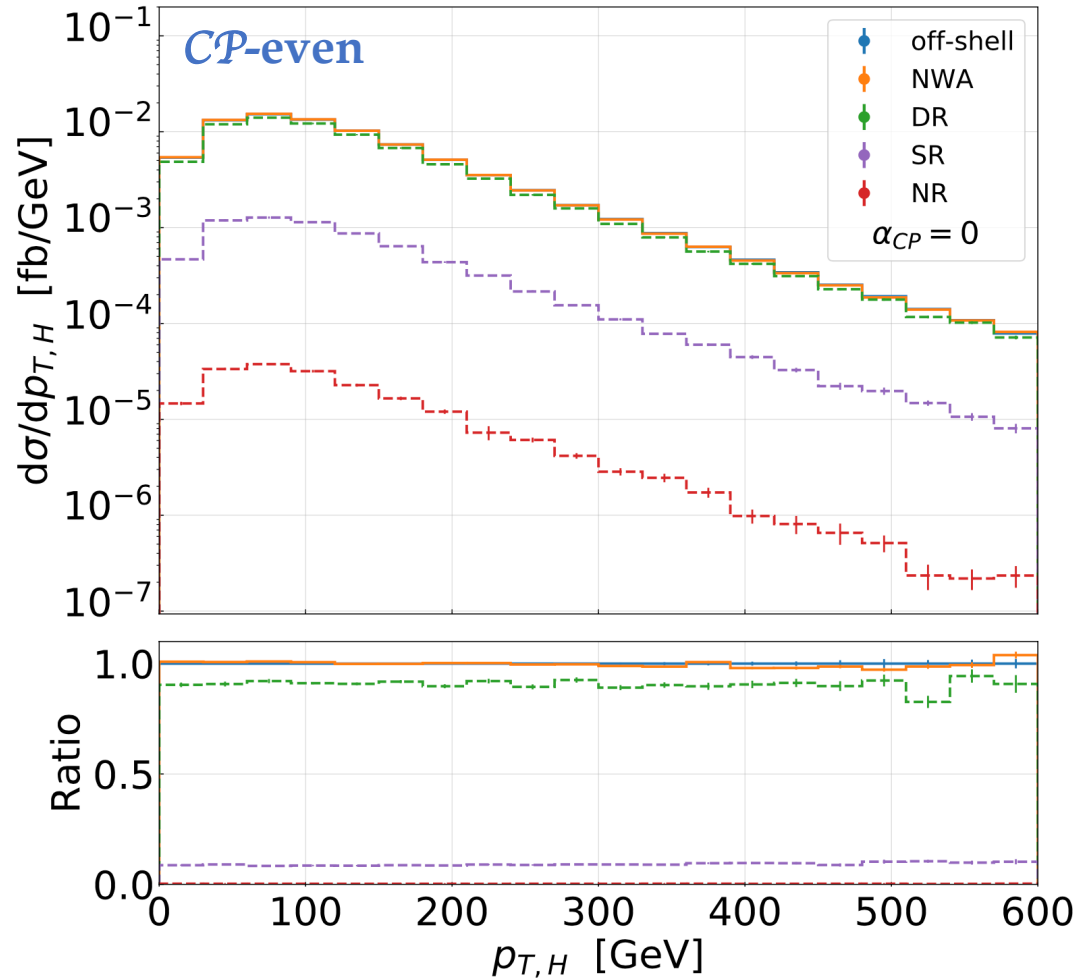
Off-shell Results: Solid line  
NWA Results: Dashed line

# Associated $tt + H$ Production

NLO  $ttH$

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} H + X$$

Hermann, Stremmer, Worek '22



SR contributions  $pp \rightarrow tWH(b)$  lead to larger off-shell effects in **CP-odd** case

# Summary

- **PROPER MODELING OF TOP-QUARK PRODUCTION & DECAY ESSENTIAL FOR**  $pp \rightarrow t\bar{t} + X, X = \gamma, Z, W^\pm, H$ 
  - Already now & already in presence of inclusive cuts
- **IMPORTANT**
  - Corrections to production & decays important  $\Leftrightarrow$  NLO  $t\bar{t}$  spin correlations
  - Photon emission in production and decays
  - Possibility of using kinematic-dependent  $\mu_R$  &  $\mu_F$  scale settings important
  - Complete off-shell effects important  $\Leftrightarrow$  Single top-quark contributions and interference effects
    - ✓ *Kinematical edges & high  $p_T$  regions*
    - ✓ *Phase space regions that are relevant for BSM physics*
- **EVEN MORE IMPORTANT FOR**
  - Exclusive cuts & High luminosity measurements
  - New Physics searches & Exclusion limits
  - SM parameter extraction
- Top quarks play important role in virtually every LHC analysis  $\Leftrightarrow$  **SM & BSM**
- Lots of data, sophisticated analyses, precision measurements  $\Leftrightarrow$  Should be compared to precise theoretical predictions



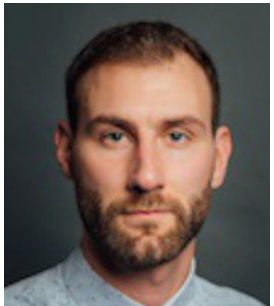
# Outlook

- What can be done with such state-of-the-art fixed order calculations ?
- Compare directly to LHC data in fiducial phase space regions
  - Have been done @ NNLO in QCD in NWA for  $pp \rightarrow t\bar{t}$  predictions *Czakon, Mitov, Poncelet '21*  
*CMS-PAS-TOP-20-006*
  - Have been done @ NLO in QCD for  $pp \rightarrow t\bar{t}\gamma$   $pp \rightarrow tW\gamma$  predictions with full off-shell effects included *ATLAS '20*  
*CERN-EP-2020-100*
  - On the way for other processes
- Provide correction to  $pp \rightarrow t\bar{t}V$  predictions matched to parton showers where
  - Approximately incorporate full off-shell effects in NLO computation of on-shell  $pp \rightarrow t\bar{t}V$  process
  - Have been done @ NLO in QCD for  $pp \rightarrow t\bar{t}W^\pm$  predictions with full off-shell effects included  
*Bevilacqua, Bi, Cordero, Hartanto, Kraus, Nasufi, Reina, Worek '22*
- Matching to parton shower programs using methods that allow for consistent treatment of resonances
  - Have been done @ NLO in QCD only for  $pp \rightarrow t\bar{t}$  predictions with full off-shell effects included  
*Jezo, Lindert, Nason, Oleari, Pozzorini '16*

## LONG TERM COLLABORATORS

- *Giuseppe Bevilacqua* (NCSR "Demokritos", Athens)
- *Huan-Yu Bi* (Peking University)
- *Heribertus Bayu Hartanto* (Cambridge University)
- *Manfred Kraus* ( National Autonomous University of Mexico)
- *Jasmina Nasufi* (Lund University)

## MY TEAM IN AACHEN



*Michele Lupattelli*



*Jonathan Hermann*



*Daniel Stremmer*



*Minos Reinartz*

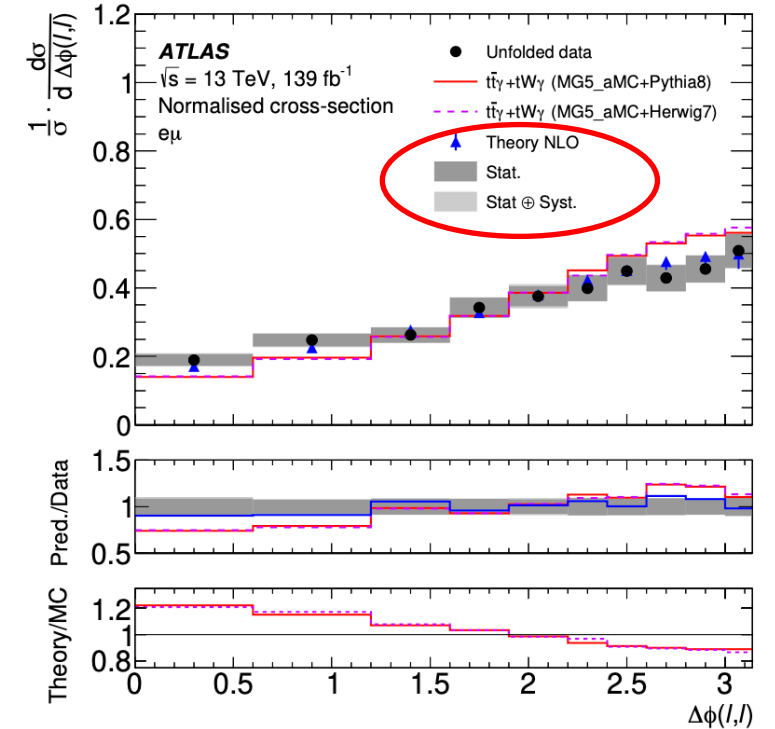
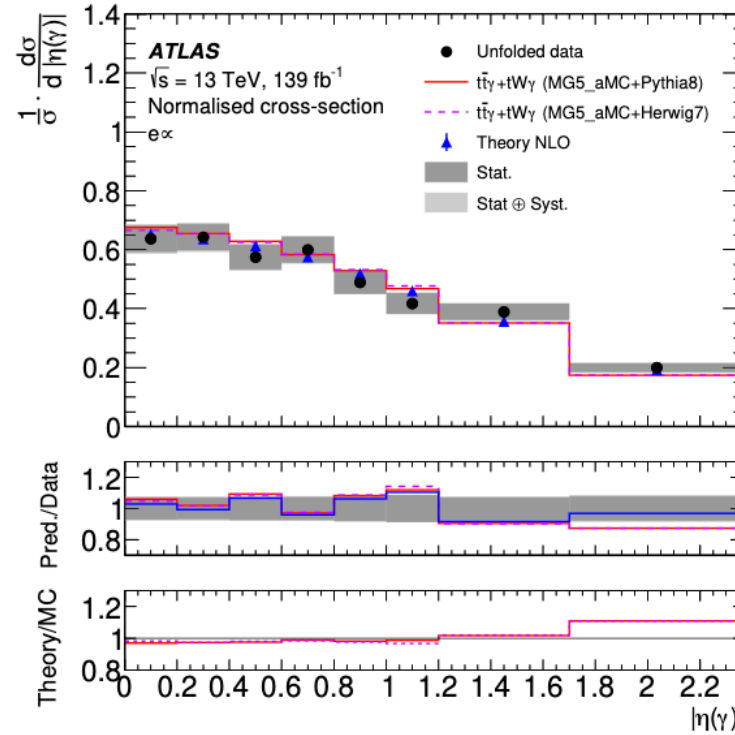
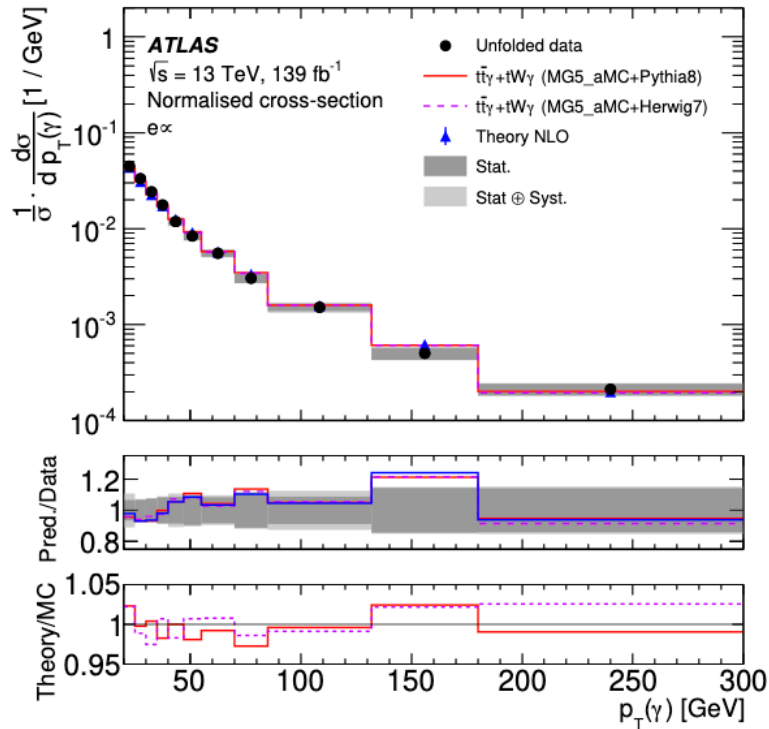


*Nikolaos Dimitrakopoulos*

BACKUP

# Associated $t\bar{t}\gamma + tW\gamma$ Production

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma + X$$



Predictions	$p_T(\gamma)$		$ \eta(\gamma) $		$\Delta R(\gamma, \ell)_{\min}$		$\Delta\phi(\ell, \ell)$		$ \Delta\eta(\ell, \ell) $	
	$\chi^2/\text{ndf}$	$p$ -value	$\chi^2/\text{ndf}$	$p$ -value	$\chi^2/\text{ndf}$	$p$ -value	$\chi^2/\text{ndf}$	$p$ -value	$\chi^2/\text{ndf}$	$p$ -value
$t\bar{t}\gamma + tW\gamma$ (MG5_aMC+PYTHIA8)	6.3/10	0.79	7.3/7	0.40	20.1/9	0.02	30.8/9	<0.01	6.5/7	0.48
$t\bar{t}\gamma + tW\gamma$ (MG5_aMC+HERWIG7)	5.3/10	0.87	7.7/7	0.36	18.9/9	0.03	31.6/9	<0.01	6.8/7	0.45
Theory NLO	6.0/10	0.82	4.5/7	0.72	13.5/9	0.14	5.8/9	0.76	5.6/7	0.59

- NLO QCD full off-shell predictions for  $t\bar{t}\gamma$
- NLO in production & decays
- NLO spin correlations

$\chi^2/\text{ndf}$  and  $p$ -values between measured normalised cross-sections and various predictions from MC simulations and NLO calculation

# Results with Full Off-Shell Effects @ LHC

- $t\bar{t}$  (di-lepton)  
*Denner, Dittmaier, Kallweit, Pozzorini '11 '12*  
*Bevilacqua, Czakon, van Hameren, Papadopoulos, Worek '11*  
*Frederix '14*  
*Heinrich, Maier, Nisius, Schlenk, Winter '14*  
*Denner, Pellen '16 (EW+QCD)*  
*Jezo, Lindert, Nason, Oleari, Pozzorini '16 (PS)*
- $t\bar{t}$  (lepton+jets)  
*Denner, Pellen '18*
- $t\bar{t}H$  (di-lepton)  
*Denner, Feger '15*
- $t\bar{t}H$  ( $H \rightarrow b\bar{b}, \tau^+\tau^-, \gamma\gamma$  &  $e^+e^-e^+e^-$ )  
*Denner, Lang, Pellen, Uccirati '17 (EW+QCD)*  
*Hermann, Stremmer, Worek '22*  
*Stremmer, Worek '22*
- $t\bar{t}j$  (di-lepton)  
*Bevilacqua, Hartanto, Kraus, Worek '16 '16*  
*Bevilacqua, Hartanto, Kraus, Worek Schulze '18*
- $t\bar{t}\gamma$  (di-lepton)  
*Bevilacqua, Hartanto, Kraus, Weber, Worek '18 '19 '20*
- $t\bar{t}Z$  &  $Z \rightarrow \nu_l \bar{\nu}_l$  (di-lepton)  
*Bevilacqua, Hartanto, Kraus, Weber, Worek '19*  
*Hermann, Worek '21*
- $t\bar{t}Z$  &  $Z \rightarrow ll$  (tetra-lepton)  
*Bevilacqua, Hartanto, Kraus, Nasufi, Worek '22*
- $t\bar{t}W$  (three-lepton)  
*Bevilacqua, Bi, Hartanto, Kraus, Worek '20*  
*Denner, Pelliccioli '20*  
*Bevilacqua, Bi, Hartanto, Kraus, Nasufi, Worek '21*  
*Denner, Pelliccioli '21 (EW+QCD)*  
*Bevilacqua, Bi, Cordero, Hartanto, Kraus, Nasufi, Reina, Worek '22*
- $t\bar{t}b\bar{b}$  (di-lepton)  
*Denner, Lang, Pellen '21*  
*Bevilacqua, Bi, Hartanto, Kraus, Lupattelli, Worek '21 '22*

# Various Phase Space Regions

- 3 different resonance histories  $\Leftrightarrow$  Resolved jet at NLO gives 9 in total

(i)	$t = W^+(\rightarrow e^+\nu_e)b$	and	$\bar{t} = W^-(\rightarrow \mu^-\bar{\nu}_\mu)\bar{b}$ ,
(ii)	$t = W^+(\rightarrow e^+\nu_e)b\gamma$	and	$\bar{t} = W^-(\rightarrow \mu^-\bar{\nu}_\mu)\bar{b}$ ,
(iii)	$t = W^+(\rightarrow e^+\nu_e)b$	and	$\bar{t} = W^-(\rightarrow \mu^-\bar{\nu}_\mu)\bar{b}\gamma$

$$pp \rightarrow e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b}\gamma + X$$

*Bevilacqua, Hartanto, Kraus, Weber, Worek '20*

- Compute for each history  $Q$  and pick one that minimises  $Q$

$$Q = |M(t) - m_t| + |M(\bar{t}) - m_t|$$

- DOUBLE-RESONANT (DR)**

$$|M(t) - m_t| < n\Gamma_t, \quad \text{and} \quad |M(\bar{t}) - m_t| < n\Gamma_t$$

- TWO SINGLE-RESONANT REGIONS (SR)**

$$|M(t) - m_t| < n\Gamma_t, \quad \text{and} \quad |M(\bar{t}) - m_t| > n\Gamma_t$$

$$|M(t) - m_t| > n\Gamma_t, \quad \text{and} \quad |M(\bar{t}) - m_t| < n\Gamma_t$$

- NON-RESONANT REGION (NR)**

$$|M(t) - m_t| > n\Gamma_t, \quad \text{and} \quad |M(\bar{t}) - m_t| > n\Gamma_t$$

- BOUNDARY PARAMETER**

- Determines size of resonant region for each reconstructed top quark
- $n = 5, 10, 15$
- For  $n = 15$

$$M(t) \in (152.9, 193.5) \text{ GeV}$$

# Photon in Top-Quark Production & Decays

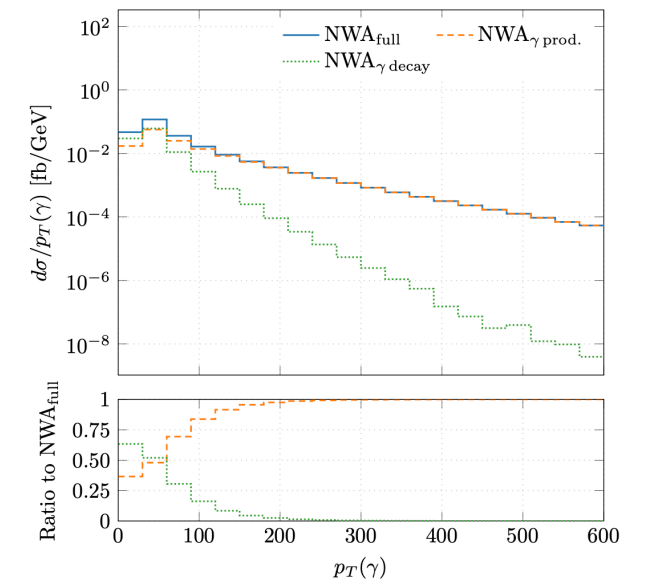
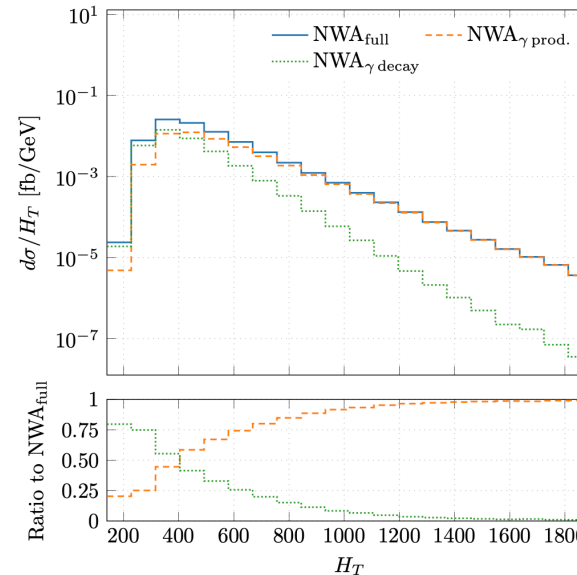
Bevilacqua, Hartanto, Kraus, Weber, Worek '18 '19 '20

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma + X$$

MODELLING APPROACH	$\sigma^{\text{LO}}$ [fb]	$\sigma^{\text{NLO}}$ [fb]
full off-shell ( $\mu_0 = H_T/4$ )	$7.32^{+2.45 (33\%)}_{-1.71 (23\%)}$	$7.50^{+0.11 (1\%)}_{-0.45 (6\%)}$
NWA ( $\mu_0 = m_t/2$ )	$8.08^{+2.84 (35\%)}_{-1.96 (24\%)}$	$7.28^{+0.99 (13\%)}_{-0.03 (0.4\%)}$
NWA ( $\mu_0 = H_T/4$ )	$7.18^{+2.39 (33\%)}_{-1.68 (23\%)}$	$7.33^{+0.43 (5.9\%)}_{-0.24 (3.3\%)}$
NWA $_{\gamma\text{-prod}}$ ( $\mu_0 = m_t/2$ )	$4.52^{+1.63 (36\%)}_{-1.11 (24\%)}$	$4.13^{+0.53 (13\%)}_{-0.05 (1.2\%)}$
NWA $_{\gamma\text{-prod}}$ ( $\mu_0 = H_T/4$ )	$3.85^{+1.29 (33\%)}_{-0.90 (23\%)}$	$4.15^{+0.12 (2.3\%)}_{-0.21 (5.1\%)}$
NWA $_{\gamma\text{-decay}}$ ( $\mu_0 = m_t/2$ )	$3.56^{+1.20 (34\%)}_{-0.85 (24\%)}$	$3.15^{+0.46 (15\%)}_{+0.03 (0.9\%)}$
NWA $_{\gamma\text{-decay}}$ ( $\mu_0 = H_T/4$ )	$3.33^{+1.10 (33\%)}_{-0.77 (23\%)}$	$3.18^{+0.31 (9.7\%)}_{-0.03 (0.9\%)}$
NWA $_{\text{LOdecay}}$ ( $\mu_0 = m_t/2$ )		$4.85^{+0.26 (5.4\%)}_{-0.48 (9.9\%)}$
NWA $_{\text{LOdecay}}$ ( $\mu_0 = H_T/4$ )		$4.63^{+0.44 (9.5\%)}_{-0.52 (11\%)}$

- For  $p_{T,b} > 40 \text{ GeV}$ 
  - 57%  $\Rightarrow$   $\gamma$  emitted in production
  - 43%  $\Rightarrow$   $\gamma$  emitted in decay stage

- NLO QCD corrections to top-quark decays
  - 12% - 17%

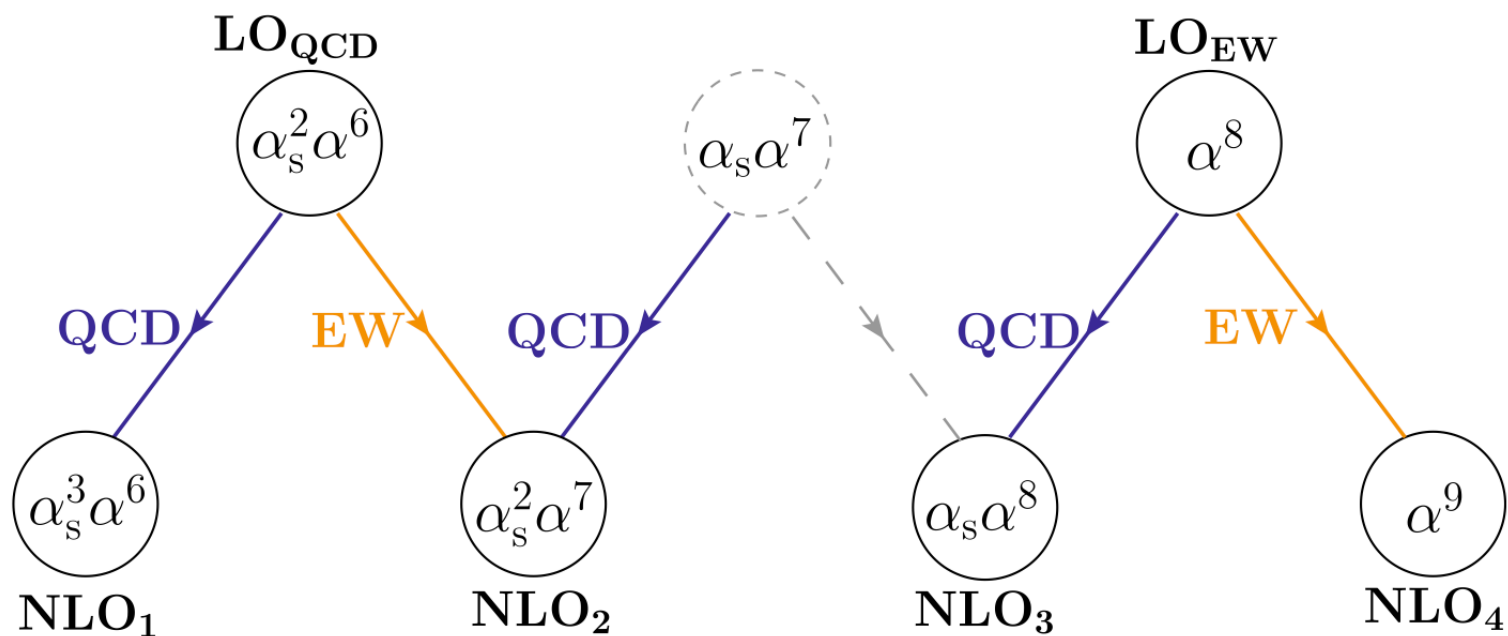




# $ttW$ & Parton Shower

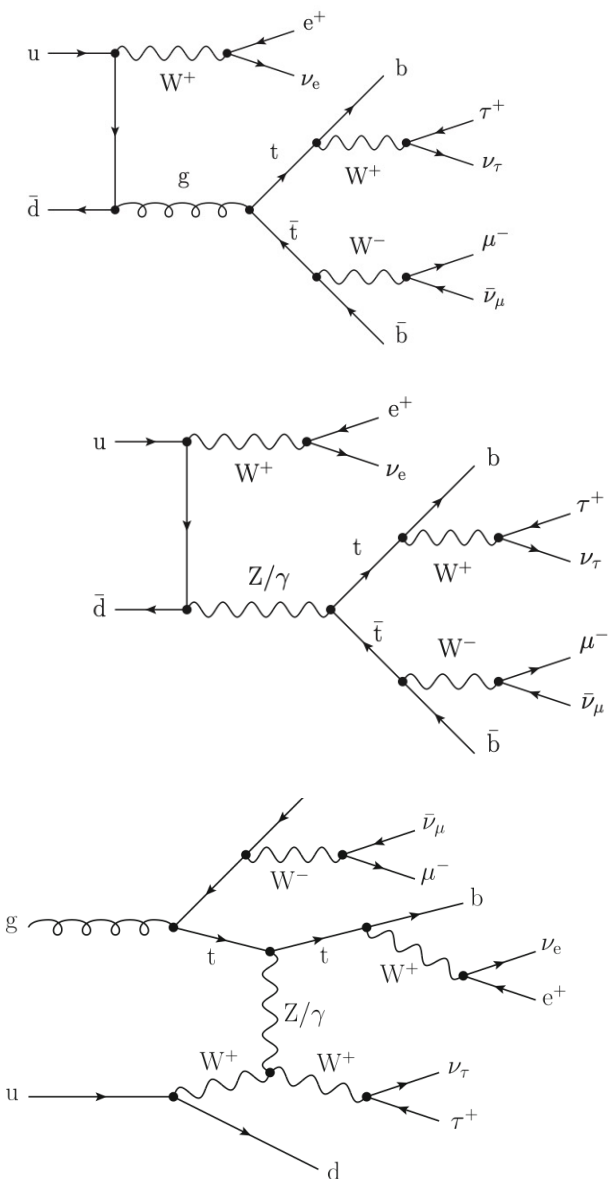
NLO  $ttW$

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu e^+ \nu_e b \bar{b}$$



$\alpha_s \alpha^8$  contribution larger than  $\alpha_s^2 \alpha^7$

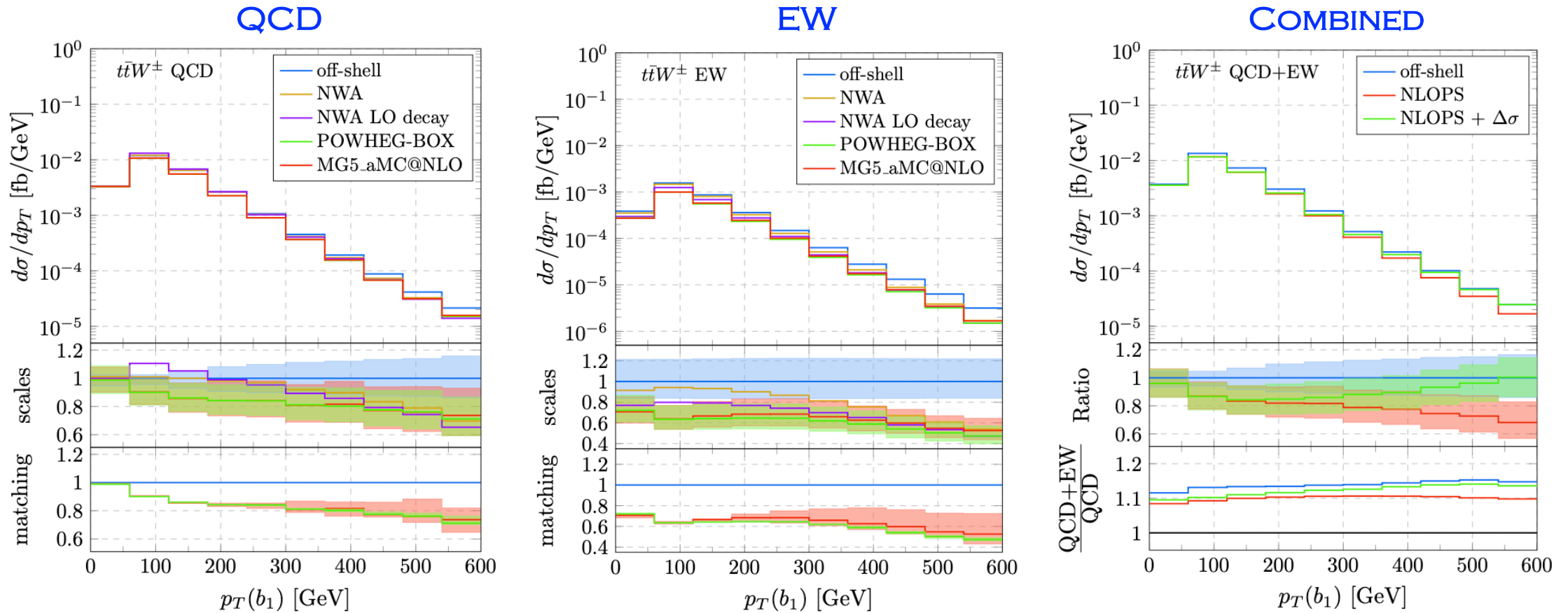
$t$ -channel  $tW \rightarrow tW$  scattering in the  $qg$  channels opens up @ NLO



# $t\bar{t}W$ & Parton Shower

NLO  $t\bar{t}W$

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu e^+ \nu_e b\bar{b} + X$$

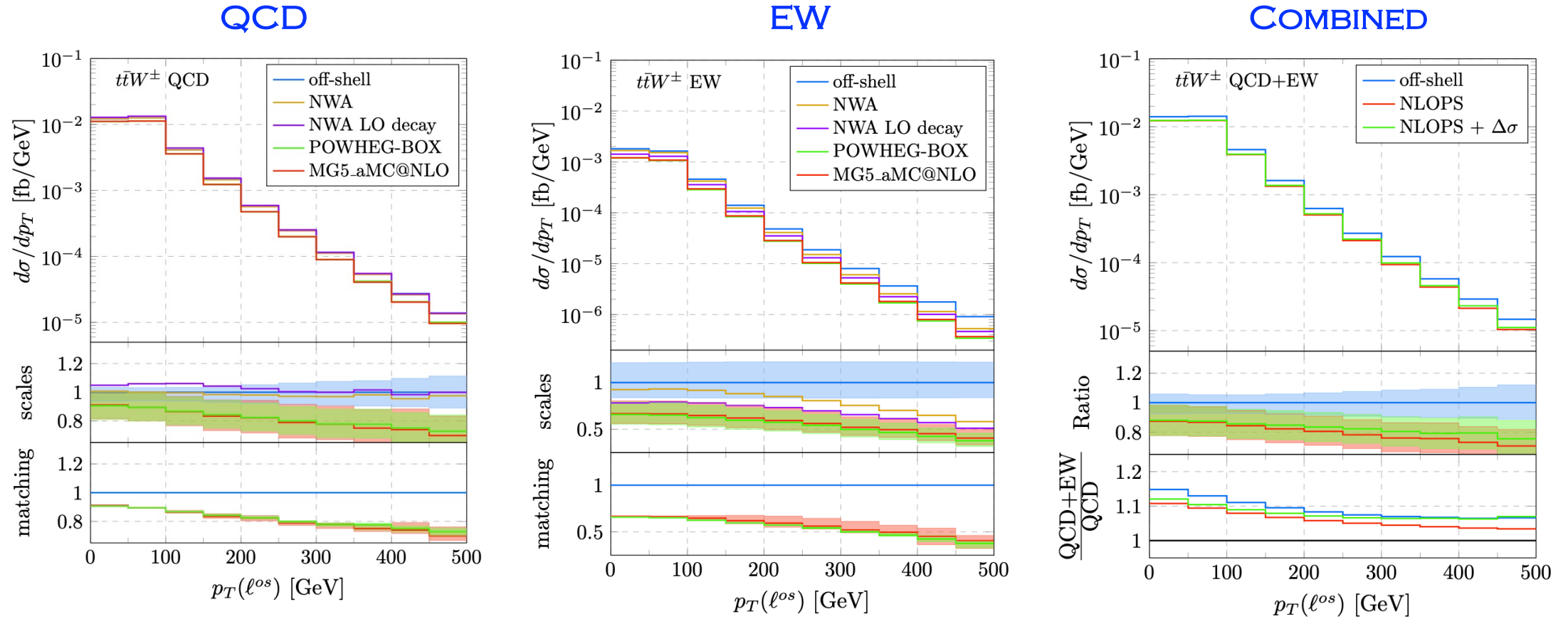


Bevilacqua, Bi, Cordero, Hartanto, Kraus, Nasufi, Reina, Worek '22

# $ttW$ & Parton Shower

NLO  $ttW$

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu e^+ \nu_e b\bar{b} + X$$



Bevilacqua, Bi, Cordero, Hartanto, Kraus, Nasufi, Reina, Worek '22

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu e^+ \nu_e b \bar{b} + X$$

Type	QCD [fb]	EW [fb]	QCD+EW [fb]	(QCD+EW)/QCD
full off-shell	$1.58^{+0.05}_{-0.10}$ (3%) (6%)	$0.206^{+0.045}_{-0.034}$ (22%) (16%)	$1.79^{+0.10}_{-0.13}$ (6%) (7%)	1.13
NLOPS	$1.40^{+0.16}_{-0.15}$ (11%) (11%)	$0.133^{+0.028}_{-0.021}$ (21%) (16%)	$1.53^{+0.19}_{-0.17}$ (12%) (11%)	1.10
NLOPS+ $\Delta\sigma$	$1.41^{+0.16}_{-0.16}$ (11%) (11%)	$0.149^{+0.028}_{-0.028}$ (19%) (19%)	$1.56^{+0.21}_{-0.21}$ (13%) (13%)	1.11

$$\frac{d\sigma^{\text{th}}}{dX} = \frac{d\sigma^{\text{NLO+PS}}}{dX} + \frac{d\Delta\sigma_{\text{off-shell}}}{dX}, \quad \text{with} \quad \frac{d\Delta\sigma_{\text{off-shell}}}{dX} = \frac{d\sigma_{\text{off-shell}}^{\text{NLO}}}{dX} - \frac{d\sigma_{\text{NWA}}^{\text{NLO}}}{dX}$$

$$\delta^{\text{th}} = \sqrt{(\delta_{\text{scale}}^{\text{NLO+PS}})^2 + (\delta_{\text{matching}}^{\text{NLO+PS}})^2 + (\delta_{\text{scale}}^{\Delta\sigma})^2}$$

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j + X$$

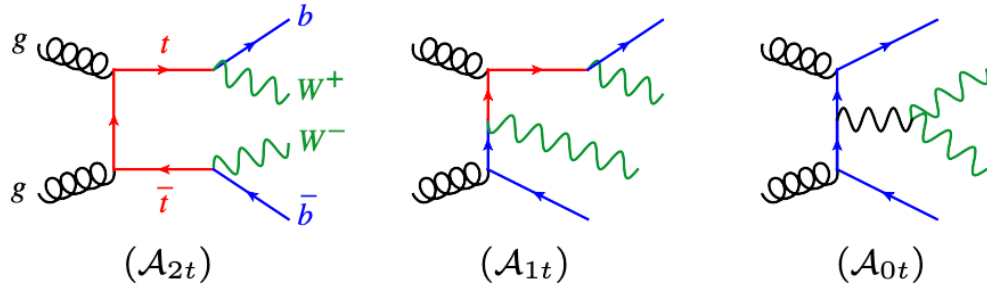
*Bevilacqua, Hartanto, Kraus, Worek '16*

Number of events, number of files & averaged number of events per file as well as total size per contribution for different **NTUPLE** samples

CONTRIBUTION	NR. OF EVENTS	NR. OF FILES	(AVG) EVENTS/FILE	SIZE
Born	$21 \times 10^6$	60	$350 \times 10^3$	38 GB
Born + Virtual	$33 \times 10^6$	380	$87 \times 10^3$	72 GB
Integrated dipoles	$80 \times 10^6$	450	$178 \times 10^3$	160 GB
Real + Sub. Real	$626 \times 10^6$	18000	$35 \times 10^3$	1250 GB
Total:	$760 \times 10^6$	18890	$40 \times 10^3$	1520 GB

# $tW(b)$

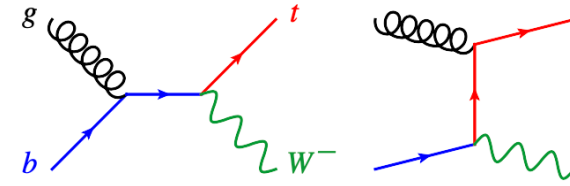
Demartin, Maier, Maltoni, Mawatari, Zaro '17



- *DS (diagram subtraction):*

$$|\mathcal{A}_{tWb}|_{\text{DS}}^2 = |\mathcal{A}_{1t} + \mathcal{A}_{2t}|^2 - \mathcal{C}_{2t},$$

- Local subtraction term  $\mathcal{C}_{2t}$  by definition must
- cancel exactly the resonant matrix element  $|\mathcal{A}_{2t}|^2$  when the kinematics is exactly on top of the resonant pole
- Be gauge invariant
- Decrease quickly away from the resonant region



- Squared matrix element for producing  $tW^{-}\bar{b}$

$$\begin{aligned} |\mathcal{A}_{tWb}|^2 &= |\mathcal{A}_{1t} + \mathcal{A}_{2t}|^2 \\ &= |\mathcal{A}_{1t}|^2 + 2\text{Re}(\mathcal{A}_{1t}\mathcal{A}_{2t}^*) + |\mathcal{A}_{2t}|^2, \end{aligned}$$

- *DR1 (without interference):*

$$|\mathcal{A}_{tWb}|_{\text{DR1}}^2 = |\mathcal{A}_{1t}|^2.$$

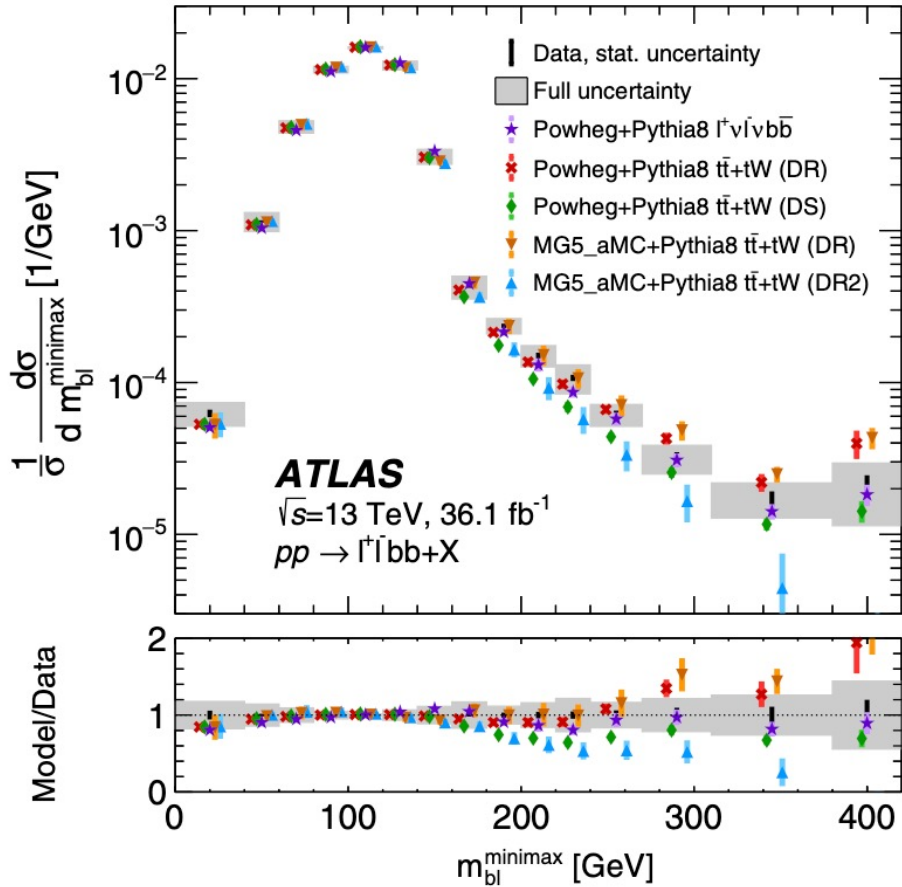
- *DR2 (with interference):*

$$|\mathcal{A}_{tWb}|_{\text{DR2}}^2 = |\mathcal{A}_{1t}|^2 + 2\text{Re}(\mathcal{A}_{1t}\mathcal{A}_{2t}^*).$$

- DR schemes based on removing contributions all over the phase space
- They are not gauge invariant

# $t\bar{t}$ & $tWb$

ATLAS '18  
ATL-PHYS-PUB-2021-042



$$m_{b\ell}^{\text{minimax}} \equiv \min\{\max(m_{b_1\ell_1}, m_{b_2\ell_2}), \max(m_{b_1\ell_2}, m_{b_2\ell_1})\}$$

$$pp \rightarrow t\bar{t} \rightarrow W^+W^-b\bar{b} \rightarrow \ell^+\nu_\ell\ell^-\bar{\nu}_\ell b\bar{b}$$

- Normalized differential  $t\bar{t}$  cross section @ NLO QCD + PS
- Full off-shell versus  $t\bar{t} + tWb \Leftrightarrow$  Di-lepton channel
- Regions sensitive to interference between doubly & singly resonant top-quark pair production
- Full off-shell prediction  $\ell^+\nu_\ell\ell^-\bar{\nu}_\ell b\bar{b}$  models well all regions
- Beyond top-quark mass traditional models of interference diverge

*p values comparing data & various MC predictions*

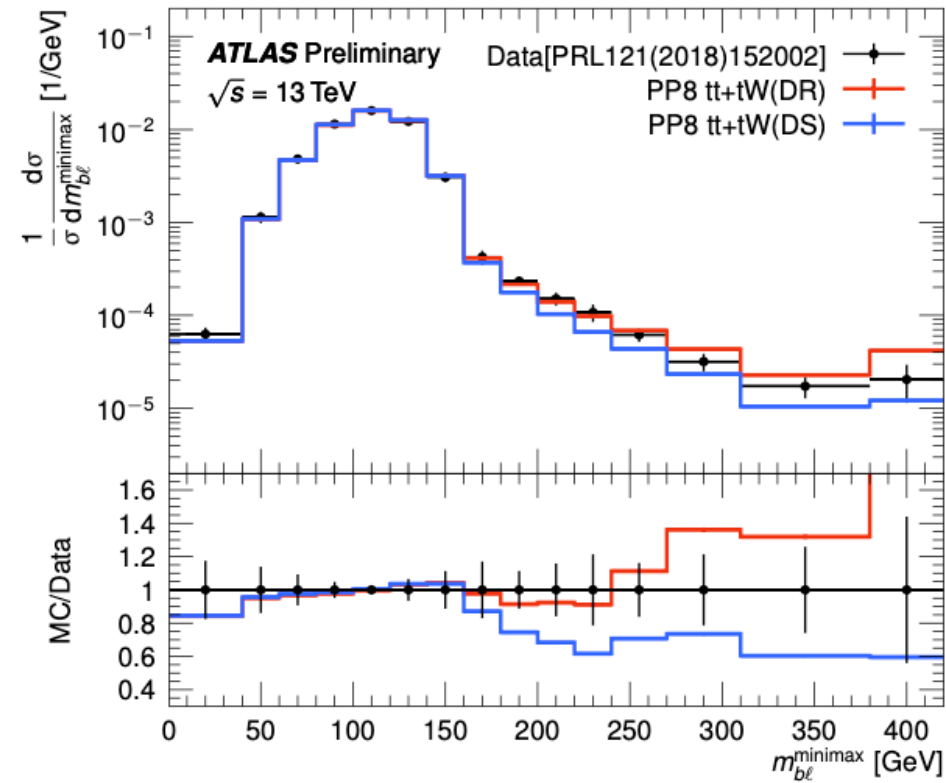
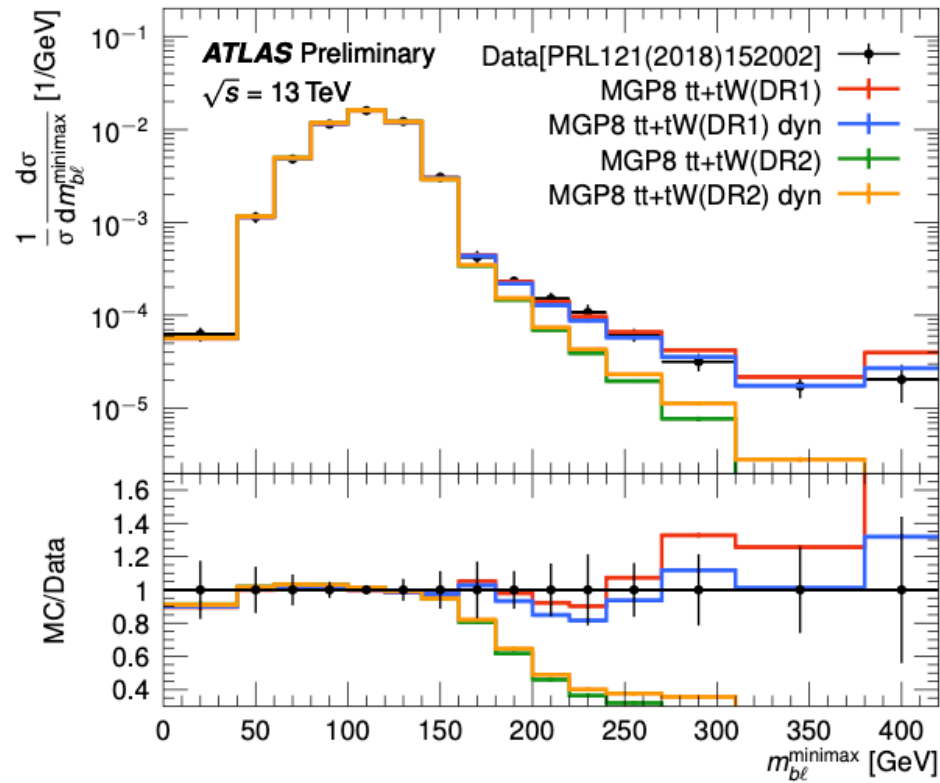
Model	All bins	$m_{b\ell}^{\text{minimax}} > 160$ GeV
POWHEG-BOX $t\bar{t} + tW$ (DR)	0.71	0.40
POWHEG-BOX $t\bar{t} + tW$ (DS)	0.77	0.56
MG5_aMC $t\bar{t} + tW$ (DR)	0.14	0.17
MG5_aMC $t\bar{t} + tW$ (DR2)	0.02	0.08
POWHEG-BOX $\ell^+\nu_\ell\ell^-\nu b\bar{b}$	0.92	0.95



# $tt$ & $tWb$

MadGraph5\_aMC@NLO+Pythia 8 (left)  
Powheg+Pythia 8 (right)

ATLAS '18  
ATL-PHYS-PUB-2021-042



*Important for proper modelling & tuning*

$$m_{b\ell}^{\text{minimax}} \equiv \min\{\max(m_{b_1\ell_1}, m_{b_2\ell_2}), \max(m_{b_1\ell_2}, m_{b_2\ell_1})\}$$